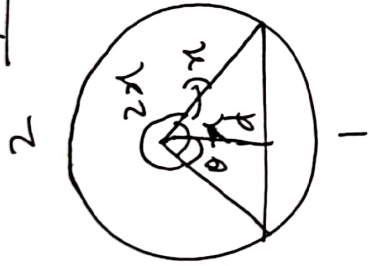


①

EQUATIONS OF CIRCLESClass: IX, MathematicsSOLUTIONSTEACHING TASK

$$2x + 2x = 360^\circ$$

$$\Rightarrow x = 120^\circ$$

$$d = \frac{|4(5) + 3(3) - 4|}{\sqrt{16+9}} = 5$$

$$\therefore \cos \theta = \frac{5}{r}$$

$$\Rightarrow \cos 60^\circ = \frac{5}{r}$$

$$\Rightarrow r = 10$$

Eqn of the circle is  $(x-5)^2 + (y-3)^2 = 100$

Ans: A

02



$$r = \sqrt{9+4} - 2 = 1$$

$$\rightarrow x+y-1=0$$



$$\frac{h-3}{1} = \frac{k-2}{1} = \frac{-2(3+2-1)}{1+1}$$

$$\therefore (h, k) = (-1, -2)$$

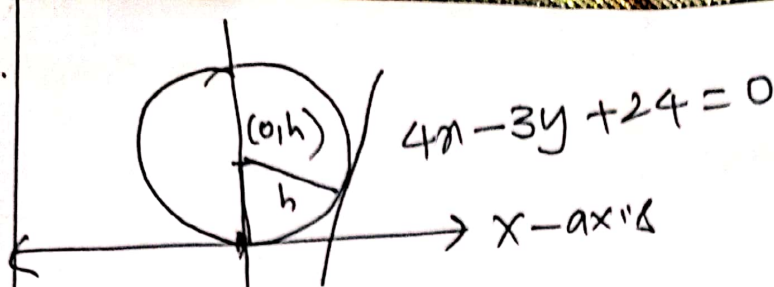
Eqn of the circle is  $(x+1)^2 + (y+2)^2 = 1^2$

$$\Rightarrow x^2 + y^2 + 2x + 4y + 4 = 0$$

Ans: A

03.

(2)



Centre =  $(0, h)$

$$h = \frac{|0 - 3h + 24|}{\sqrt{16 + 9}}$$

$$\Rightarrow 5h = |24 - 3h|$$

$$\Rightarrow 24 - 3h = \pm 5h$$

$$\Rightarrow h = 3 \text{ or } -12$$

Eqn. of the circles

Eqn of the circles  
Centre  $(0, 3)$ ,  $r = 3$   
 $(x-0)^2 + (y-3)^2 = 3^2$

$$\Rightarrow x^2 + y^2 - 6y = 0$$

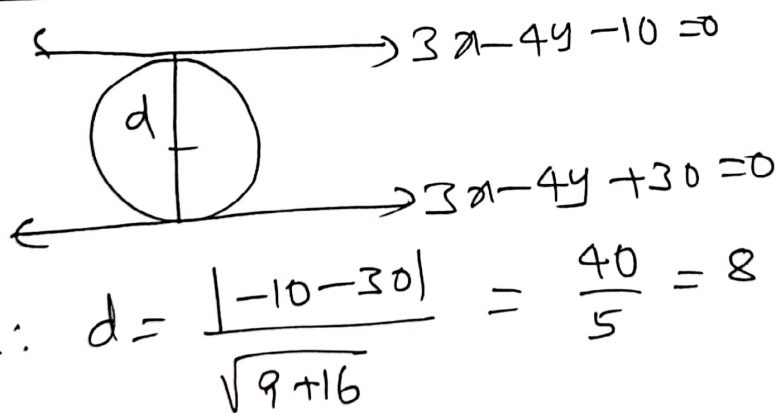
Also  $C(0, -12)$ ,  $r = 12$

$$(x-0)^2 + (y+12)^2 = (12)^2$$

$$\Rightarrow x^2 + y^2 + 24y = 0$$

Ans: A

04.



$$\therefore d = \frac{|-10 - 30|}{\sqrt{9 + 16}} = \frac{40}{5} = 8$$

$$\therefore r = 4.$$

Option Verification: A)  $x^2 + y^2 - 4x - 2y - 11 = 0$

$$r = \sqrt{4 + 1 + 11} = 4.$$

Centre  $(2, 1)$  lies on  $x - 2y = 0$ , which is true.

Ans: A

05

$$x - 2y - 3 = 0$$

$$x - 2y = 3$$

$$\Rightarrow \frac{x}{3} + \frac{y}{(-\frac{3}{2})} = 1$$

Centre  $(h, -h)$

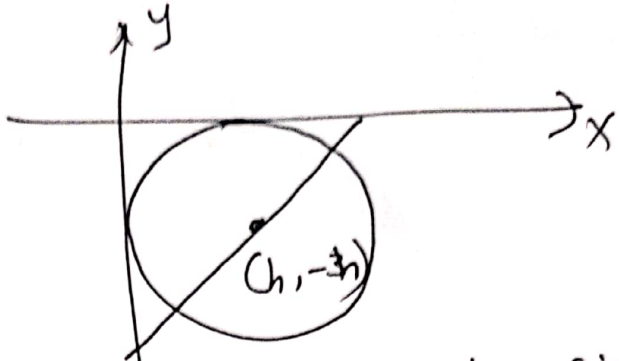
Lies on  $x - 2y - 3 = 0$

$$\Rightarrow h + 2h - 3 = 0$$

$$\Rightarrow h = 1$$

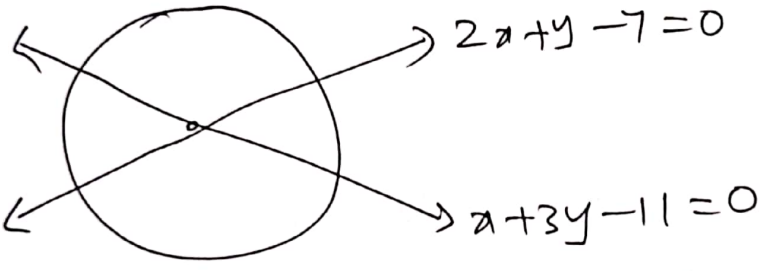
$\therefore$  Centre  $(1, -1)$

radius = 1



Ans: B

06



Solving equations, centre  $(2, 3)$ .

Circle also passes through  $(5, 7)$

$$\therefore \text{radius} = \sqrt{9 + 16} = 5$$

Eqn of the circle  $(x-2)^2 + (y-3)^2 = 5^2$

$$\Rightarrow x^2 + y^2 - 4x - 6y - 12 = 0$$

Ans: C

07.  $3x - 2y + 6 = 0$

$\Rightarrow 3x - 2y = -6$

$\Rightarrow \frac{3x}{-6} - \frac{2y}{-6} = 1$

$\Rightarrow \frac{x}{-2} + \frac{y}{3} = 1$

$\therefore A(-2, 0), B(0, 3)$

$AB = \sqrt{(0+2)^2 + (3-0)^2}$   
 $= \sqrt{4+9}$   
 $= \sqrt{13}$

④

Eq<sup>n</sup> of the circle  $(x+2)^2 + (y-0)^2 = (\sqrt{13})^2$

$\Rightarrow x^2 + y^2 + 4x - 9 = 0$

Ans: B

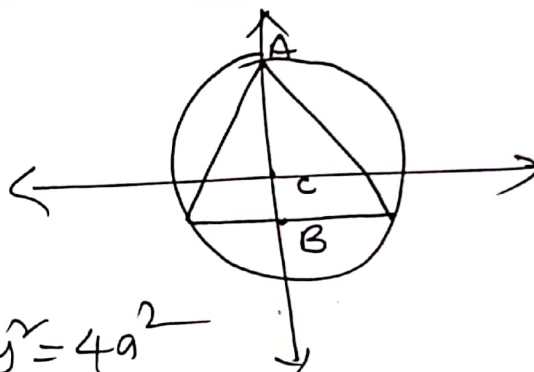
08

$AB = 3a$

We know  $AC : CB = 2 : 1$

$\therefore AC = r = \frac{2}{3} \times 3a = 2a$

$\therefore$  Eq<sup>n</sup> of the circle  $\Rightarrow x^2 + y^2 = 4a^2$



09. Circle passes through  $(2, 0)$  and  $(0, 4)$

mid-point =  $(1, 2)$

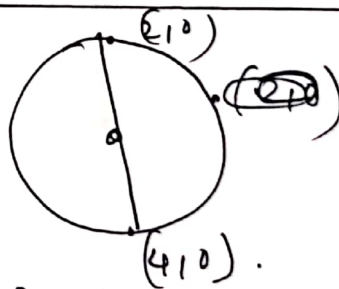
Eq<sup>n</sup> of the circle  $(x-1)^2 + (y-2)^2 = r^2$

Circle passes through  $(2, 0) \Rightarrow (2-1)^2 + (0-2)^2 = r^2$   
 $\Rightarrow 1+4 = r^2 \Rightarrow r^2 = 5$

$\therefore$  Eq<sup>n</sup> of the circle  $(x-1)^2 + (y-2)^2 = r^2 = 5$

$\Rightarrow x^2 + y^2 - 2x - 4y = 0$

Ans: B



10.

$$x = \frac{2a(1-t^2)}{1+t^2}, \quad y = \frac{4at}{1+t^2}$$

put  $t = \tan \theta$

$$\therefore x = \frac{2a(1-\tan^2 \theta)}{1+\tan^2 \theta}, \quad y = \frac{2a(2 \tan \theta)}{1+\tan^2 \theta}$$

$$\Rightarrow x = 2a \cdot \cos 2\theta, \quad y = 2a \cdot \sin 2\theta$$

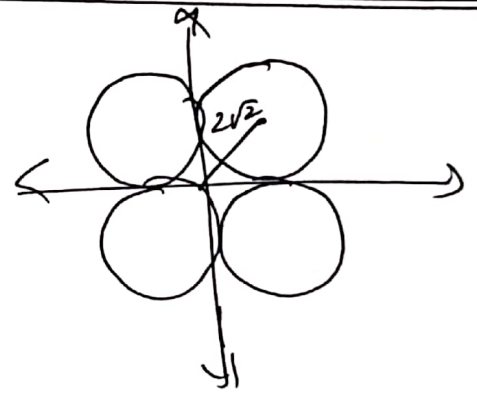
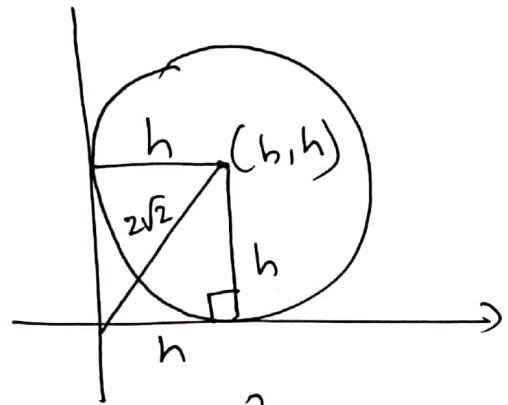
$$\Rightarrow \frac{x}{2a} = \cos 2\theta, \quad \frac{y}{2a} = \sin 2\theta$$

$$\Rightarrow x^2 + y^2 = (2a)^2$$

hence radius = 2a

Ans: B

11.



$$h^2 + h^2 = (2\sqrt{2})^2$$

$$\Rightarrow h = \pm 2$$

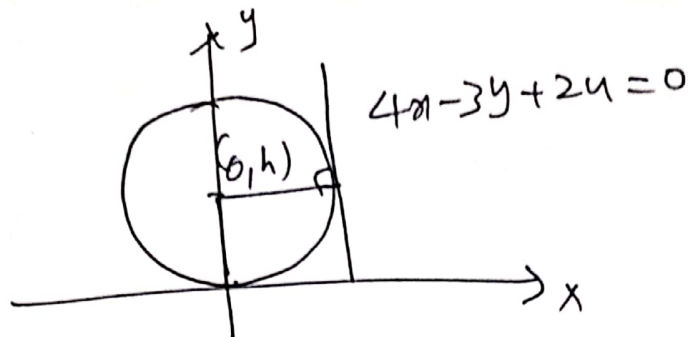
The centres are  $(2, 2), (2, -2), (-2, 2), (-2, -2)$

radius =  $r = 2$

Hence the equations of the circles are all the four options satisfies

Ans: A, B, C, D

12.



$$\text{radius} = h = \frac{|4 \cdot 0 - 3h + 24|}{\sqrt{16 + 9}}$$

$$\Rightarrow 5h = |24 - 3h|$$

$$\Rightarrow \pm 5h = 24 - 3h$$

$$\Rightarrow h = 3 \text{ or } -12$$

Eqn of the circles (6)

Centre (0, 3),  $r = 3$ 

$$\Rightarrow x^2 + y^2 - 6y = 0$$

Also  $c(0, -12)$ ,  
 $r = 12$ 

Eqn of the circle

$$x^2 + y^2 + 24y = 0$$

Ans: B, D

13. Statement I:

$$r = \frac{|5(4) - 12(3) - 10|}{\sqrt{5^2 + (-12)^2}}$$

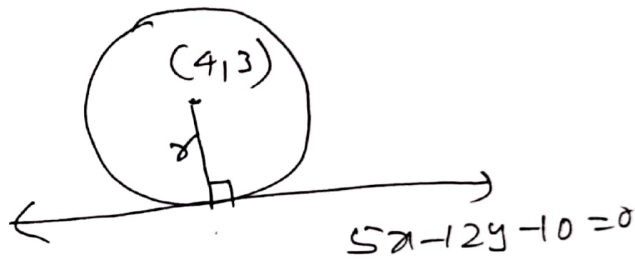
$$\therefore r = 2.$$

$\therefore$  Eqn of the circle  $(x-4)^2 + (y-3)^2 = 2^2$

$$\Rightarrow x^2 + y^2 - 8x - 6y + 21 = 0. \text{ (True)}$$

Statement II: Conceptual (True)

Ans: A

14. Statement I:  $(4, -1)$  radius =  $|k| = |-1| = 1$   
 $(h, k)$ 

$$\therefore (x-4)^2 + (y+1)^2 = 1^2 \Rightarrow x^2 + y^2 - 8x + 2y + 16 = 0 \text{ (True)}$$

Statement II: Conceptual (True)

Ans: A

15.

$$x^2 + y^2 = 16$$

Centre = (0,0), r = 4.

parametric Equations

$$x = r \cos \theta, \quad y = r \sin \theta$$

$$x = 4 \cos \theta, \quad y = 4 \sin \theta$$

Ans: A

16

$$x^2 + y^2 + 2x + 4y - 11 = 0$$

Centre = (-1, -2)

$$\text{radius} = r = \sqrt{1 + 4 + 11} = 4.$$

parametric Equations

$$x = h + r \cos \theta, \quad y = k + r \sin \theta$$

$$\Rightarrow x = -1 + 4 \cos \theta, \quad y = -2 + 4 \sin \theta$$

Ans: C

17

$$3x + 4y = 12$$

$$\Rightarrow \frac{x}{4} + \frac{y}{3} = 1$$

$$\therefore A(x_1, y_1), B(x_2, y_2)$$

Eqn of the circle

$$(x-4)(x-0) + (y-0)(y-3) = 0$$

$$\Rightarrow x^2 - 4x + y^2 - 3y = 0$$

$$\Rightarrow x^2 + y^2 - 4x - 3y = 0$$

Ans: D

18

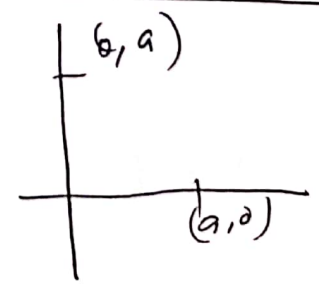
$$A(0, a), B(a, 0), AB = \sqrt{a^2 + a^2}$$

$$= \sqrt{2a^2}$$

$$= \sqrt{2} a$$

Eqn of the circle

$$(x - \frac{a}{2})^2 + (y - \frac{a}{2})^2 = (\sqrt{2} a)^2$$



18  $A(a, 0), B(0, a)$

(8)

$$AB = \sqrt{a^2 + a^2} = \sqrt{2a^2} = \sqrt{2}a.$$

$\therefore$  Diameter =  $d = \sqrt{2}a$

mid-point of  $AB = \left(\frac{a}{2}, \frac{a}{2}\right)$

Eq<sup>n</sup> of the circle

$$\left(x - \frac{a}{2}\right)^2 + \left(y - \frac{a}{2}\right)^2 = \left(\frac{\sqrt{2}a}{2}\right)^2$$

$$\Rightarrow 2x^2 + 2y^2 - 2ax - 2ay - 3a^2 = 0$$

Ans: B

19  $x^2 - 4x - 6 = 0$

Let  $x_1, x_2$  be the roots

We have  $x_1 + x_2 = 4$  ;  $x_1 \cdot x_2 = -6$

Also,  $y^2 + 2y - 7 = 0$

Let  $y_1, y_2$  be the roots

$$\Rightarrow y_1 + y_2 = -2, y_1 \cdot y_2 = -7$$

Eq<sup>n</sup> of the circle

$$(x - x_1)(x - x_2) + (y - y_1)(y - y_2) = 0$$

$$\Rightarrow x^2 + y^2 - (x_1 + x_2)x + x_1 x_2 + y^2 - (y_1 + y_2)y + y_1 y_2 = 0$$

$$\Rightarrow x^2 + y^2 - 4x - 6 + y^2 + 2y - 7 = 0$$

$$\Rightarrow x^2 + y^2 - 4x + 2y - 13 = 0$$

$$x^2 + y^2 + 2ax + 2by + c = 0$$

$$a = -2, b = 1, c = -13$$

$$4a + b - c = -2 + 1 + 13$$

$$= 12$$

Ans: 12



20

$$A(0, 1), B(\alpha, \beta)$$

Eqn of the circle is

$$(x-0)(x-\alpha) + (y-1)(y-\beta) = 0$$

$$\Rightarrow x^2(x-\alpha) + (y-1)(y-\beta) = 0$$

This circle cuts the  $x$ -axis, put  $y=0$

$$\Rightarrow x(x-\alpha) + \beta = 0$$

$$\Rightarrow x^2 - \alpha x + \beta = 0$$

$$\Rightarrow x^2 - 5x + 3 = 0$$

$$\Rightarrow \alpha = 5, \beta = 3 \quad \therefore \alpha + \beta = 8$$

Ans: 8

21. a)  ~~$x^2 + y^2 + ax + by + 2b^2 = 0$  touches  $x$ -axis~~

~~Since  $(x + \frac{a}{2})^2 + (y + \frac{b}{2})^2 = (\frac{b}{2})^2$~~

21 a)  $x^2 + y^2 + 2ax - 2by + a^2 = 0$  touches  $x$ -axis

Since  $g^2 = c$  i.e.  $a^2 = a^2$

b)  $x^2 + y^2 - 2ax + 2by + b^2 = 0$  touches  $y$ -axis

Since  $f^2 = c$  i.e.  $b^2 = b^2$

c)  $x^2 + y^2 + 2ax + 2ay + a^2 = 0$  touches both the axes

Since  $g^2 = f^2 = c$  i.e.  $a^2 = a^2 = a^2$

d)  $x^2 + y^2 + ax - by - 2a^2 = 0$  passes through  $(a, b)$

Since  $a^2 + b^2 + a^2 - b^2 - 2a^2 = 0$

Ans: b, c, d



22 a)  $x = \frac{2a(1-t^2)}{1+t^2}$ ,  $y = \frac{4at}{1+t^2}$

put  $t = \tan \theta$

$x = 2a \cdot \cos 2\theta$ ,  $y = 2a \cdot \sin 2\theta$

$\Rightarrow x^2 + y^2 = 4a^2 = (2a)^2$   
 $\therefore$  Radius =  $2a$

b)  $x = 5 \cos \theta$ ,  $y = 5 \sin \theta$

Eqn of the circle  $\Rightarrow x^2 + y^2 = 25 \rightarrow \textcircled{1}$

$\theta = 135^\circ$ , Slope =  $m = \tan \theta = \tan 135^\circ = -1$ .

C  $(-\sqrt{8}, \sqrt{8})$

Eqn of the circle  $y - \sqrt{8} = -1(x + \sqrt{8})$   
 $\Rightarrow y - \sqrt{8} = -x - \sqrt{8}$   
 $\Rightarrow x + y = 0$   
 $\Rightarrow x = -y \rightarrow \textcircled{2}$

Solving  $\textcircled{1}$  &  $\textcircled{2}$   $x^2 + x^2 = 25 \Rightarrow 2x^2 = 25$   
 $\Rightarrow x = \pm \frac{5}{\sqrt{2}}$

$\therefore y = \mp \frac{5}{\sqrt{2}}$

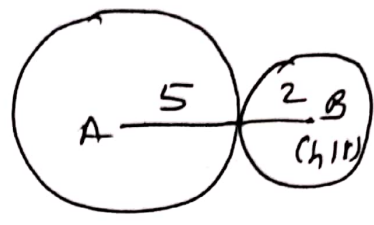
$\therefore A(\frac{5}{\sqrt{2}}, -\frac{5}{\sqrt{2}})$ ,  $B(-\frac{5}{\sqrt{2}}, \frac{5}{\sqrt{2}})$

$\therefore AB = \sqrt{(\frac{10}{\sqrt{2}})^2 + (\frac{10}{\sqrt{2}})^2} = 10$

c)

c) Circle eqn.

$$x^2 + y^2 - 4x - 6y - 12 = 0$$



$$C = (2, 3), \quad B = (h, k)$$

$$r = \sqrt{4 + 9 + 12}$$

$$r = 5$$

$$\therefore AB = 5 + 2 = 7$$

$$\Rightarrow (2 - h)^2 + (3 - k)^2 = 49$$

$$\Rightarrow h^2 + k^2 - 4h - 6k - 36 = 0$$

$$\therefore \Rightarrow x^2 + y^2 - 4x - 6y - 36 = 0$$

Ans: 9

d)  $3x - 4y = 12$

$$\Rightarrow \frac{x}{4} + \frac{y}{-3} = 1$$

Centre  $(h, -h)$

$$h = \frac{|3h + 4h - 12|}{\sqrt{9 + 16}}$$

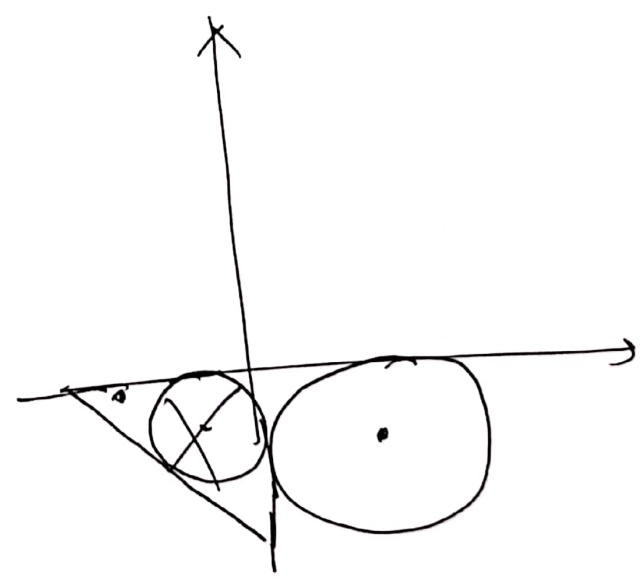
$$\Rightarrow 5h = |7h - 12|$$

$$\Rightarrow \pm 5h = 7h - 12$$

$$\Rightarrow h = 6 : \text{Centre } (6, -6), r = 6$$

Eqn of  $(x - 6)^2 + (y + 6)^2 = 6^2$

$$\Rightarrow x^2 + y^2 - 12x + 12y = 0$$



$$d) 3x - 4y = 12$$

$$\Rightarrow \frac{x}{4} + \frac{y}{-3} = 1$$

Centre  $(h, -h)$ ,  $r = h$

$$h = \frac{|3h + 4h - 12|}{\sqrt{9 + 16}}$$

$$\Rightarrow 5h = |7h - 12|$$

$$\Rightarrow 7h - 12 = \pm 5h$$

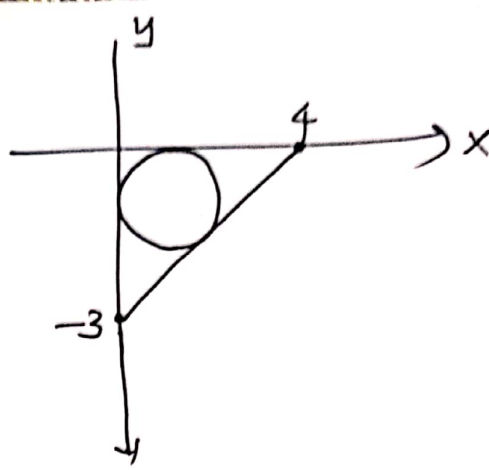
$$\Rightarrow h = 6 \text{ or } 1$$

Centre  $(6, -6)$ ,  $r = 6$

Eqn of the circle

$$(x-6)^2 + (y+6)^2 = 6^2$$

$$\Rightarrow x^2 + y^2 - 12x + 12y + 36 = 0$$



(12)

Centre  $(1, -1)$ ,  $r = 1$

$$(x-1)^2 + (y+1)^2 = 1^2$$

$$\Rightarrow x^2 + y^2 - 2x + 2y + 1 = 0$$

Q

d)  $3x - 4y = 12$

$\Rightarrow \frac{x}{4} + \frac{y}{-3} = 1$

Centre  $(h, -h), r = h$

$h = \frac{|3h + 4h - 12|}{\sqrt{9 + 16}}$

$\Rightarrow 5h = |7h - 12|$

$\Rightarrow 7h - 12 = \pm 5h$

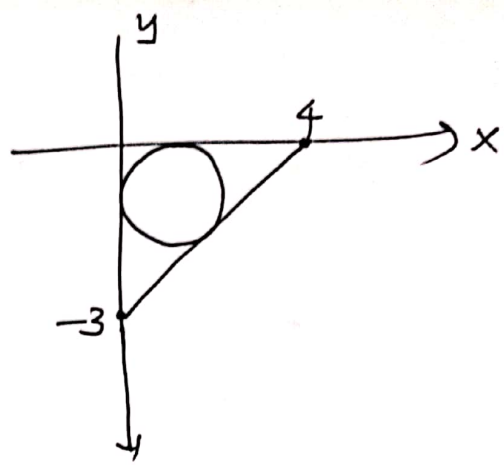
$\Rightarrow h = 6 \text{ or } 1$

Centre  $(6, -6), r = 6$

Eqn of the circle

$(x-6)^2 + (y+6)^2 = 6^2$

$\Rightarrow x^2 + y^2 - 12x + 12y + 36 = 0$



(12)

Centre  $(1, -1), r = 1$

$(x-1)^2 + (y+1)^2 = 1^2$

$\Rightarrow x^2 + y^2 - 2x + 2y + 1 = 0$

## LEARNERS TASK

### CUG's

01. opt: B.  $x^2 + y^2 - 6x + 12y - 15 = 0$

$g = -3, f = 6, c = -15$

$g^2 + f^2 - c \geq 0$

$\Rightarrow 9 + 36 + 15 \geq 0.$

Ans: B

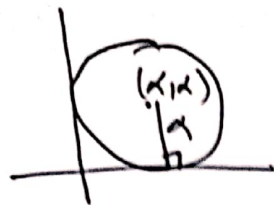
02. Conceptual (c)

Ans: C

03. Conceptual (D)

Ans: D

04.



Eqn of the circle

$$(x-x_1)^2 + (y-y_1)^2 = r^2$$

Ans: A

(13)

05

$$x^2 + y^2 - 6x + 2y + 15 = 0 \Rightarrow \text{Centre } (3, -1)$$

$$x^2 + y^2 - 6x + 12y - 15 = 0 \Rightarrow \text{Centre } (3, -6) \text{ Ans: A}$$

06

$$ax^2 + ay^2 + 2gx + 2fy + c = 0$$

$$\Rightarrow x^2 + y^2 + \frac{2g}{a}x + \frac{2f}{a}y + \frac{c}{a} = 0$$

$$\text{Centre} = \left(-\frac{g}{a}, -\frac{f}{a}\right)$$

Ans: C

07 Conceptual (D)

Ans: D.

08 Conceptual (D)

Ans: D

09

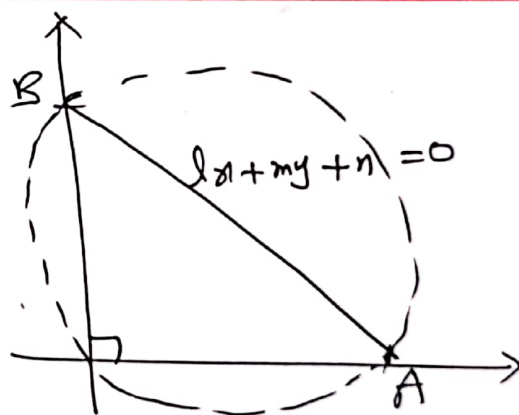
$$lx + my + n = 0$$

$$\Rightarrow lx + my = -n$$

$$\Rightarrow \frac{x}{\left(-\frac{n}{l}\right)} + \frac{y}{\left(-\frac{n}{m}\right)} = 1$$

$$\therefore A\left(-\frac{n}{l}, 0\right), B\left(0, -\frac{n}{m}\right)$$

$x_1 \quad y_1 \qquad \qquad \qquad x_2 \quad y_2$



Eqn of the circle

$$\left(x + \frac{n}{l}\right)(x - 0) + (y - 0)\left(y + \frac{n}{m}\right) = 0$$

$$\Rightarrow x^2 + \frac{n}{l}x + y^2 + \frac{n}{m}y = 0$$

$$\Rightarrow lm(x^2 + y^2) + n(mx + ly) = 0$$

Ans: B

10 Conceptual (B)

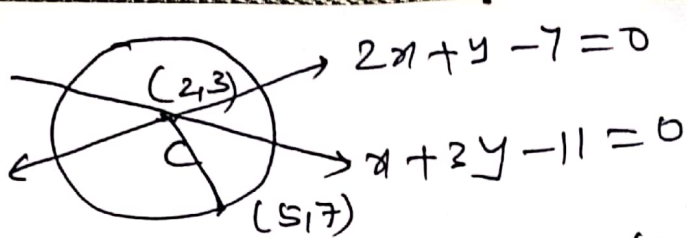
JEE MAINS QUESTIONS

~~Q1.  $x^2 + y^2 - 6x + 12y + 15 = 0$   
 radius =  $\sqrt{9 + 36 - 15}$  | Centre =  $(3, -6)$   
 $= \sqrt{30}$   
 Eqn of the circle  $(x-3)^2 + (y+6)^2 = (2\sqrt{30})^2$   
 $\Rightarrow x^2 + y^2 - 6x + 12y + 9 + 36 - 120 = 0$   
 $\Rightarrow x^2 + y^2 - 6x + 12y$~~

01.  $x^2 + y^2 - 6x + 12y + 15 = 0$   
 radius =  $\sqrt{9 + 36 - 15}$  | Centre =  $(3, -6)$   
 $= \sqrt{30}$   
 Area =  $\pi r^2 = 30\pi$   
 Double Area =  $60\pi = \pi R^2 \Rightarrow R^2 = 60$   
 Eqn of the circle  $(x-3)^2 + (y+6)^2 = 60$   
 $\Rightarrow x^2 + y^2 - 6x + 12y + 9 + 36 - 60 = 0$   
 $\Rightarrow x^2 + y^2 - 6x + 12y - 15 = 0$  Ans. A

02  $3x - 2y + 6 = 0$  | : A(-2, 0), B(0, 3)  
 $\Rightarrow 3x - 2y = -6$  |  $r = AB = \sqrt{4 + 9} = \sqrt{13}$   
 $\Rightarrow \frac{x}{-2} + \frac{y}{3} = 1$   
 Eqn of the circle  $(x+2)^2 + (y-0)^2 = (\sqrt{13})^2$   
 $\Rightarrow x^2 + y^2 + 4x + 4 - 13 = 0 \Rightarrow x^2 + y^2 + 4x - 9 = 0$  Ans. B

03



(15)

Solving equations, centre (2,3)

Circle passes through (5,7)

$$\therefore \text{radius} = \sqrt{(5-2)^2 + (7-3)^2}$$

$$= \sqrt{9+16} = 5$$

Eqn of the circle  $(x-2)^2 + (y-3)^2 = 5^2$

$$\Rightarrow x^2 + y^2 - 4x - 6y + 4 + 9 - 25 = 0$$

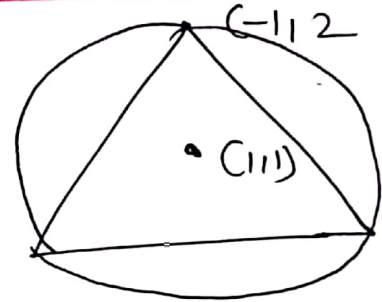
$$\Rightarrow x^2 + y^2 - 4x - 6y - 12 = 0$$

Ans: C

04

For equilateral triangle

Centroid = Circumcentre = (1,1)



$$\therefore \text{radius} = \sqrt{(1+1)^2 + (1-2)^2}$$

$$= \sqrt{4+1} = \sqrt{5}$$

Eqn of the circle  $(x-1)^2 + (y-1)^2 = (\sqrt{5})^2$

$$\Rightarrow x^2 + y^2 - 2x - 2y + 1 + 1 - 5 = 0$$

$$\Rightarrow x^2 + y^2 - 2x - 2y - 3 = 0$$

05

Circle passes through (2,0), (0,4)

mid-point = (1,2)

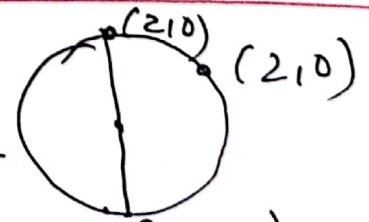
Eqn of the circle =  $(x-1)^2 + (y-2)^2 = r^2$

Circle passes through (2,0)  $\Rightarrow (2-1)^2 + (0-2)^2 = r^2$

$$\Rightarrow r^2 = 5$$

Eqn of the circle  $\Rightarrow x^2 + y^2 - 2x - 4y = 0$

Ans: B





06.  $(x-1)^2 + (y+2)^2 = 9$

(16)

centre =  $(1, -2)$ ,  $r = 3$

parametric point =  $(h + r \cos \theta, k + r \sin \theta)$   
 $= (1 + 3 \cos \theta, -2 + 3 \sin \theta)$  Ans: B

07.  $2x + 3y + 1 = 0$

$\Rightarrow 2x + 3y = -1$

$\Rightarrow \frac{x}{(-\frac{1}{2})} + \frac{y}{(\frac{-1}{3})} = 1$

$A(-\frac{1}{2}, 0), B(0, -\frac{1}{3})$

$6x + 4y + 1 = 0$

$\Rightarrow \frac{x}{(\frac{-1}{6})} + \frac{y}{(\frac{-1}{4})} = 1$

$C(-\frac{1}{6}, 0), D(0, -\frac{1}{4})$

opt: A  $\rightarrow 12x^2 + 12y^2 + 8x + 7y + 1 = 0$  satisfies

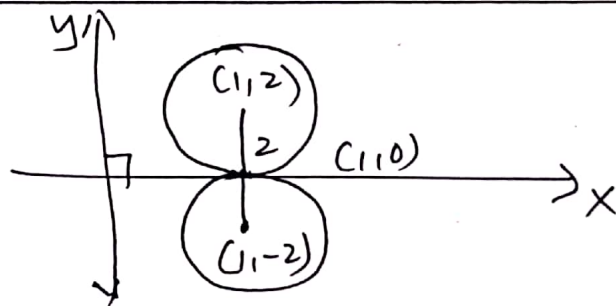
the above points

Ans: A

08

Centres may be

$(1, 2)$  &  $(1, -2)$



09.  $x-2=0$

$\Rightarrow x=2$

~~$x^2 + y^2 - 8x - 2y = 0$~~

~~$4 + y^2 - 16 - 2y = 0$~~

~~$\Rightarrow y^2 - 2y - 12 = 0$~~

~~$\Rightarrow (y+2)(y-6) = 0 \Rightarrow y = -2, 6$~~

09.  $x-2=0$

$x=2$

$x^2 + y^2 - 8x - 2y = 0$

$\Rightarrow 4 + y^2 - 16 - 2y = 0$

$\Rightarrow y^2 - 2y - 12 = 0 \Rightarrow y = 1 \pm \sqrt{13}$

$A(2, 1 + \sqrt{13}), B(2, 1 - \sqrt{13})$  satisfies option: A

i.e.  $x^2 + y^2 - 4x - 2y = 0$

Ans: B

10

$$x = \frac{8t}{1+t^2} \quad \left| \quad y = 4 \left( \frac{1-t^2}{1+t^2} \right) \right. \quad (17)$$

$$x = 4 \left( \frac{2t}{1+t^2} \right)$$

put  $t = \tan \theta$ 

$$\therefore x = 4 \sin 2\theta, \quad y = 4 \cos 2\theta$$

$$x^2 + y^2 = 16$$

This is a circle with centre  $(0,0)$ , radius = 4

Ans. B

11

$$ax^2 + by^2 + 3y^2 - 5x + 2y - 3 = 0 \rightarrow \text{Circle}$$

$$a=3, \quad b=0$$

$$\therefore 3x^2 + 3y^2 - 5x + 2y - 3 = 0$$

$$\Rightarrow x^2 + y^2 - \frac{5}{3}x + \frac{2}{3}y - 1 = 0$$

$$\text{Centre} = \left( \frac{5}{6}, -\frac{1}{3} \right)$$

$$\text{radius} = \sqrt{\frac{25}{36} + \frac{1}{9} + 1} = \frac{\sqrt{65}}{6}$$

Ans A, B, C, D

12

$$3x^2 + 3y^2 - 5x - 6y + 4 = 0$$

$$\Rightarrow x^2 + y^2 - \frac{5}{3}x - 2y + \frac{4}{3} = 0$$

$$\text{Centre} = \left( \frac{5}{6}, 1 \right)$$

$$\text{radius} = \sqrt{\frac{25}{36} + 1 - \frac{4}{3}} = \frac{\sqrt{13}}{6}$$

Ans: A, B

$$13 \xrightarrow{\text{SI:}} x + 3y - 1 = 0, \quad x + y + 1 = 0, \quad 2x + 3y + 4 = 0$$

Solving  $A(-2, 1), B(1, -2), C(-5, 2)$

All these points satisfy  $x^2 + y^2 + 12x + 12y + 7 = 0$

St. II: Conceptual (True)

Ans. A



14. statement I: Centre lies on X-axis

(18)

Let the centre be  $C(h, 0)$

Let  $A(-2, 3)$ ,  $B(4, 5)$



We have  $CA = CB$

$$\Rightarrow CA^2 = CB^2$$

$$\Rightarrow (h+2)^2 + (0-3)^2 = (h-4)^2 + (0-5)^2$$

$$\Rightarrow h^2 + 4h + 4 + 9 = h^2 - 8h + 16 + 25$$

$$\Rightarrow 12h = 28 \Rightarrow h = \frac{7}{3}$$

$\therefore$  Centre =  $(\frac{7}{3}, 0)$ .

Given eqn  $3(x^2 + y^2) - 14x - 67 = 0$

$$\Rightarrow x^2 + y^2 - \frac{14}{3}x - \frac{67}{3} = 0$$

Centre  $(\frac{7}{3}, 0)$  also this eqn satisfies

A and B.

Statement II: Conceptual (true)

Ans: A

15  $(x+a)^2 + (y+b)^2 = a^2 + b^2$

$$\Rightarrow x^2 + y^2 + 2ax + 2by + 2b^2 = 0$$

Ans: B

16  $(x - \cos\theta)^2 + (y - \sin\theta)^2 = 1$

$$\Rightarrow x^2 + y^2 - 2\cos\theta x - 2\sin\theta y = 0$$

Ans: D

17 Eqn of the circle passing through  $(1, 2)$ ,  $(3, -4)$

and  $(5, -6)$  is  $x^2 + y^2 - 22x - 2y + 25 = 0$

$$(C18) \Rightarrow c^2 + 64 - 22c - 16 + 25 = 0$$

$$\Rightarrow c^2 - 22c + 57 = 0 \Rightarrow c = 3, 19$$

Ans: D

18. Eqn of the circle passing through  $(2,0), (0,1), (4,5)$  is  $3(x^2+y^2) - 13x - 17y + 14 = 0$  (19)

$$(0,c) = 3(0+c^2) - 13(0) - 17c + 14 = 0$$

$$\Rightarrow 3c^2 - 17c + 14 = 0$$

$$\Rightarrow c = \frac{14}{3}$$

Ans: C

19.  $C(2,3), A(2,-1)$

$$r = CA$$

$$r^2 = CA^2 = (2-2)^2 + (3+1)^2 = 16$$

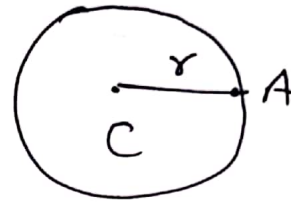
$$\therefore (x-2)^2 + (y-3)^2 = 16$$

$$\Rightarrow x^2 + y^2 - 4x - 6y + 3 = 0$$

$$x^2 + y^2 + ax + by + c = 0$$

$$\Rightarrow a + b + c = -4 - 6 + 3 = -13$$

Ans: -13



20.  $A(1,2), B(2,a)$

$$c = \left( \frac{1+2}{2}, \frac{2+a}{2} \right)$$

$$c = \left( \frac{3}{2}, \frac{2+a}{2} \right)$$

Eqn of the circle

$$(x-1)(x-2) + (y-2)(y-a) = 0$$

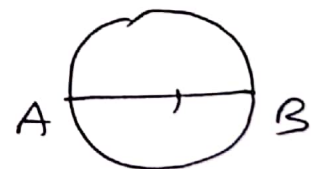
$$\Rightarrow x^2 - 3x + 2 + y^2 - ay - 2y + 2a = 0$$

$$\Rightarrow x^2 + y^2 - 3x - (a+2)y + 2 + 2a = 0$$

$$x^2 + y^2 - 3x + 4y + 6 = 0$$

$$\therefore -(a+2) = 4 \Rightarrow a = -2$$

Ans: 2



21) 1) Centre  $(\frac{3}{2}, \frac{1}{2})$

Circle  $\Rightarrow x^2 + y^2 - 3x - y + 1 = 0$

2) Centre  $(0,0)$ , passing through  $(-1, 2)$

$\therefore r = \sqrt{1+4} = \sqrt{5}$

$\therefore x^2 + y^2 = 5$

3)  $x^2 + y^2 + 3x + 4y + 6 = 0$

4)  $(x+1)^2 + (y+1)^2 = 49$

Centre  $(-1, -1) \Rightarrow$   
radius = 7

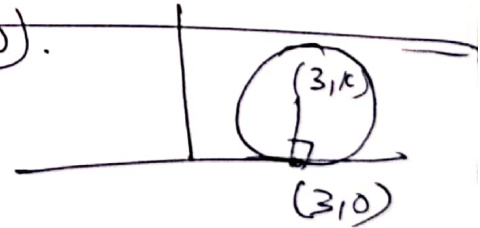
~~$x+y=0$~~  Satisfies  
 $2x - 3y = 5$   
 $3x - 4y = 7$

Area =  $\pi r^2$   
 $= \frac{22}{7} \times 7^2 = 154$

22) 1) Circle touches x-axis at  $(3,0)$ .

$\therefore$  Centre  $(3, k)$ , A  $(1, -2)$

radius  $r = \sqrt{(3-1)^2 + (k+2)^2}$   
 $= \sqrt{\quad}$

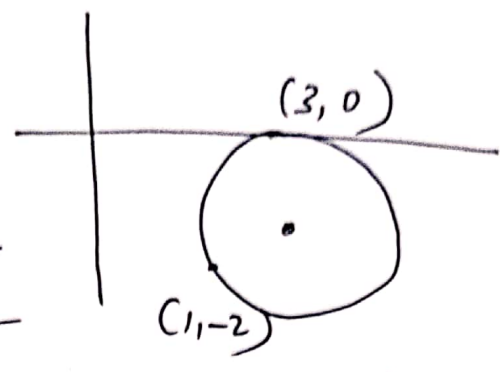


22

1) Centre (3, k)  
radius = k.

Eqn of the circle

$$(x-3)^2 + (y-k)^2 = k^2$$



This circle passes through (1, -2)

$$(1-3)^2 + (-2-k)^2 = k^2$$

$$\Rightarrow k = -2$$

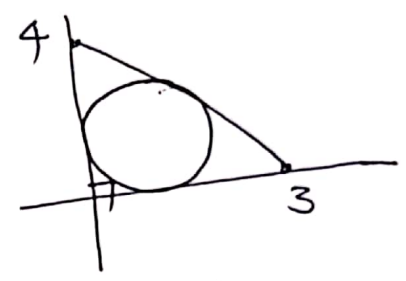
∴ Eqn of the circle  $(x-3)^2 + (y+2)^2 = 4$ .

∴ (5, -2) satisfies the above eqn.

2)  $4x + 3y = 12$

$$\Rightarrow \frac{x}{3} + \frac{y}{4} = 1$$

Centre (r, r), radius = r



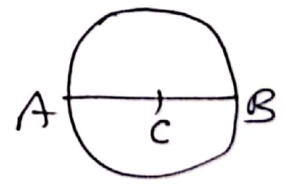
$$r = \frac{|4r + 3r - 12|}{\sqrt{9 + 16}}$$

$$\Rightarrow \pm 5r = 7r - 12$$

$$\Rightarrow r = 6$$

$$\Rightarrow 5r = |7r - 12|$$

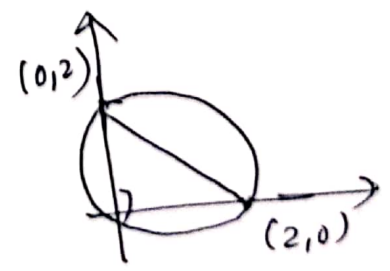
3) A(2, 3), C(4, 4), B(x, y)



$$\frac{2+x}{2} = 4 \quad \Bigg| \quad \frac{3+y}{2} = 4$$

$$\therefore (x, y) = (6, 5)$$

4) A(2, 0), B(0, 2)  
mid-point = (1, 1)



⇒ THE END ⇐

Ans: 1, 1, 1, 2