

6th - ws-5
Foundation 7 Basic

①

$$\text{side } a = 1 \text{ m}, \quad m = 3 \text{ kg}$$

$$\text{volume of cube} = a^3 = 1^3 = 1$$

$$\text{density} = \frac{\text{mass}}{\text{volume}} = \frac{3}{1} = 3 \text{ kg/m}^3$$

②

$$\text{volume} = 25 \text{ m}^3; \quad \text{density} = 5 \text{ kg/m}^3$$

$$\text{mass} = \text{density} \times \text{volume}$$

$$= 5 \times 25 = 125 \text{ kg}$$

③

$$\text{mass} = 50 \text{ gm} = 50 \times 10^{-3} \text{ kg}, \quad \text{R.D} = 10$$

$$\text{Relative density} = \frac{\text{density of a body}}{\text{density of water}}$$

$$\Rightarrow 10 = \frac{d_b}{10^3} \Rightarrow d_b = 10 \times 10^3$$

$$\Rightarrow d_b = 10^4$$

$$\text{volume} = \frac{m}{d_b} = \frac{50 \times 10^{-3}}{10^4} = 50 \times 10^{-7} \text{ m}^3$$

$$= 5 \times 10^{-6} \text{ m}^3 = 5 \text{ cm}^3$$

(4)

$$\text{mass} = 500 \text{ kg} ; \text{volume} = 0.5 \text{ m}^3$$

$$d_w = 10^3 \quad d_{\text{body}} = \frac{m}{V} = \frac{500}{0.5} = 10^3 \text{ kg/m}^3$$

$$\text{Relative density} = \frac{d_{\text{body}}}{d_{\text{water}}} = \frac{10^3}{10^3} = 1$$

(5)

$$m_1 = 30 \text{ kg} ; \text{vol}_1 = 3 \text{ m}^3$$

$$m_2 = 15 \text{ kg} ; \text{vol}_2 = 2 \text{ vol}_1 = 2 \times 3 = 6 \text{ m}^3$$

$$\therefore \text{change in density} = d_2 \sim d_1$$

$$= \frac{m_2}{\text{vol}_2} \sim \frac{m_1}{\text{vol}_1}$$

$$= \frac{15}{6} \sim \frac{30}{3} \Rightarrow \frac{15 \sim 60}{6}$$

$$= \frac{45}{6} = \frac{15}{2} = 7.5 \text{ kg/m}^3$$

(6)

$$m_1 = 5 \text{ kg} ; m_2 = 3 \text{ kg}$$

density = same.

$$\frac{V_1}{V_2} = \frac{m_1}{m_2} = \frac{5}{3}$$

(7)

$$V_1 = 2 \text{ m}^3 ; V_2 = 4 \text{ m}^3$$

mass = same.

Density $\propto \frac{1}{\text{volume}}$

$$\Rightarrow \frac{d_1}{d_2} = \frac{V_2}{V_1} = \frac{4}{2} = \frac{2}{1}$$

8

$$mass = 100 \text{ gm} = 10^{-1} \text{ kg} \quad ; \quad V_b$$

$$\begin{aligned} \text{volume of water displaced} &= 20 \sim 40 = 20 \text{ cm}^3 \\ &= 20 \times 10^{-6} \text{ m}^3 \end{aligned}$$

$$\text{loss of weight of the body} = \text{weight of water displaced}$$

$$\Rightarrow d_b V_b g = d_w \times V_{\text{liquid displaced}} g$$

$$\Rightarrow m_b d_b = d_w \times 20 \times 10^{-6}$$

$$\Rightarrow \frac{10^{-1} \times 10^6}{20} = d_w \Rightarrow d_w = 5 \times 10^3 \text{ gm/cc} = 5 \text{ kg/m}^3$$

9

$$m_1 = 1 \text{ kg} \quad ; \quad m_2 = 2 \text{ kg}$$

$$R.D. = \frac{d_{\text{body}}}{d_{\text{water}}} = \frac{m_b}{V_b d_{\text{water}}}$$

$$\frac{R.D._1}{R.D._2} = \frac{m_{b_1}}{m_{b_2}} = \frac{1}{2}$$

10

$$mass = 20 \text{ kg} \quad ; \quad V = 10 \text{ m}^3$$

in order to float on water

$$d_b = d_w$$

$$R.D. = \frac{d_b}{d_w}$$

$$\Rightarrow \frac{m_{b_1} + m_{b_2}}{V} = 10^3$$

$$\Rightarrow \frac{20 + m}{10} = 10$$

(14)

$$m_{b_1} = 2 \text{ kg} \quad d_b = 10 \text{ kg/m}^3$$

$$m_{b_2} = 2m_{b_1} \quad d_b = ? \quad d \propto m$$

$$\Rightarrow \frac{d_{b_1}}{d_{b_2}} = \frac{m_{b_1}}{m_{b_2}}$$

$$\Rightarrow \frac{10}{d_{b_2}} = \frac{m_{b_1}}{2m_{b_1}} = \frac{1}{2}$$

$$\Rightarrow d_{b_2} = 2 \times 10 = 20 \text{ kg/m}^3$$

(15)

$$vol_1 = 2 \text{ m}^3$$

$$d_1 = 5 \text{ kg/m}^3$$

$$vol_2 = 1 \text{ m}^3$$

$$d_2 = ?$$

$$\Rightarrow d \propto \frac{1}{V} \quad \Rightarrow \frac{d_1}{d_2} = \frac{V_2}{V_1} \quad \Rightarrow \frac{5}{d_2} = \frac{1}{2}$$

$$\Rightarrow d_2 = 10 \text{ kg/m}^3$$

(16)

$$m_1 = 5 \text{ kg} \quad V = 2 \text{ m}^3$$

$$d_{\text{sphere}} = \frac{m}{V} = \frac{5}{2} = 2.5 \text{ kg/m}^3$$

(17)

$$m = 20 \text{ gm} \quad ; \quad vol = 4 \text{ cm}^3 \quad ; \quad d_w = 1 \text{ gm/cc}$$

$$R \cdot d = \frac{d_b}{d_w} = \frac{\frac{m}{V}}{d_w} = \frac{\frac{20}{4}}{1} = \frac{m}{V d_w}$$

$$R \cdot d < 1 \quad \Rightarrow d_b < d_w$$

$$\text{Volume of body} = R \cdot d \cdot V = \frac{m}{d_w} \cdot \frac{m}{R \cdot d}$$

$$\text{Here } R \cdot d < 1 \quad \text{if we take } V \text{ value as } 25 \quad R \cdot d = \frac{20}{25 \times 1} = \frac{4}{5} < 1$$

(18)

$$\text{side} = 0.5 \text{ m}$$

$$m = 2 \text{ kg}$$

$$\text{density} = \frac{m}{\text{vol}} = \frac{2 \text{ m}}{(\text{side})^3}$$

$$= \frac{2}{(0.5)^3} = \frac{2}{125 \times 10^{-3}} = \frac{2 \times 10^3}{125}$$

$$= 2 \times \frac{1000}{125} = 16 \text{ kg/m}^3$$

(19)

$$\text{density} = 20 \text{ kg/m}^3$$

$$\text{volume} = 4 \text{ m}^3$$

$$\therefore \text{mass} = \text{density} \times \text{volume} = 20 \times 4 = 80 \text{ kg}$$

L Task
SAQA

(1)

$$\text{vol} = 3 \text{ m}^3 ; \quad \text{mass} = 30 \text{ kg}$$

$$\text{density} = \frac{m}{V} = \frac{30}{3} = 10 \text{ kg/m}^3$$

(2)

$$m = 400 \text{ kg}; \quad \text{vol} = 2 \text{ m}^3 ; \quad d_w = 1000 \text{ kg/m}^3$$

$$R.d = \frac{d_{\text{body}}}{d_w} = \frac{200}{1000}$$

$$d_b = \frac{m}{V} = \frac{400}{2} = 200$$

$$R.d = 0.2$$

③

$$vol = 10 \text{ cm}^3 \quad ; \quad d = 2 \text{ gm/cm}^3$$

$$mass = d \times vol = 2 \times 10 = 20 \text{ gm}$$

④

$$m_{cube} = 2 \text{ kg} \quad ; \quad m_{cuboid} = 5 \text{ kg}$$

we know density & mass

$$\Rightarrow \frac{d_{cube}}{d_{cuboid}} = \frac{m_{cube}}{m_{cuboid}} = \frac{2}{5}$$

⑤

$$V_1 = 6 \text{ cm}^3 \quad ; \quad V_2 = 9 \text{ cm}^3$$

$$\text{Relative density} = \frac{d_{body}}{d_{water}} = \frac{\frac{m_{body}}{V_{body}}}{d_{water}}$$

$$\frac{R.D_1}{R.D_2} = \frac{V_2}{V_1} = \frac{9}{6} = \frac{3}{2}$$

⑥

$$mass = 300 \text{ kg} \quad ; \quad R.d = 0.03 \quad ; \quad d_w = 10^3 \text{ kg/m}^3$$

$$\text{Relative density} = \frac{m_{body}}{V_{body} \times d_{water}}$$

$$V_{body} = \frac{m_{body}}{R.D \times d_w} = \frac{300}{0.03 \times 10^3} = 10 \text{ m}^3$$

7

$$d = 5\text{m}; r = 1\text{m}; \text{density} = \rho \quad \text{mass} = 20\text{ kg}$$

$$\text{volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 1^2 \times 5$$

$$= \frac{110}{7}$$

$$\text{density} = \frac{\text{mass}}{\text{Volume}} = \frac{20}{\frac{110}{7}} = \frac{2 \times 7}{11} = \frac{14}{11}$$

$$= 1.27 \text{ kg/m}^3$$

8

$$1\text{cm}; r = \text{vol}_{\text{liquid}} = 125 \text{ cm}^3 \quad m_{\text{L}} = 250 \text{ gm}$$

$$m_{\text{empty beaker}} = 100 \text{ gm} \quad \therefore m_{\text{L}} + m_{\text{empty beaker}} = 250 \text{ gm}$$

$$\times m_{\text{liquid}} = 250 - m_{\text{empty beaker}} \\ = 250 - 100 = 150 \text{ gm}$$

$$\text{density of liquid} = \frac{m_{\text{liquid}}}{\text{vol}} = \frac{150}{125} = \frac{6}{5} = 1.2 \text{ cm}^3$$

9

$$m = 0.02 \text{ gm} \quad ; \quad \text{vol} = 2 \text{ cm}^3 \quad ; \quad d_w = 1 \text{ gm/cc}$$

if the brick sink in water $d_b > d_w$

$$d_b = \frac{m}{\text{vol}} = \frac{0.02}{2} = 0.01 \text{ gm/cc} < d_w \quad \therefore \text{so if the volume of body} < \text{it's original volume then } d_b > d_w$$

$$\text{for } V = 0.02, \text{ we will get } d_b = \frac{0.02}{0.02} = 1.0 > d_w$$

(10)

$$d_{\text{cube}} = 0.8 \text{ kg/m}^3 \quad ; \quad m = 10 \text{ kg}$$

if the cube wants to sink in water

$$d_b > d_w$$

$$\text{we know } d_w = 1 \text{ gm/cc} = 10^3 \text{ kg/m}^3$$

$\therefore d_b = 2000 \text{ kg/m}^3$ then only it can sink in water

(13)

$$l \times b \times h = 4 \text{ cm} \times 1 \text{ cm} \times 5 \text{ cm} \quad ; \quad m = 50 \text{ gm}$$

$$= 20 \times \text{cm}^3 \quad d_w = 1 \text{ gm/cc}$$

$$\text{Relative density} = \frac{m_b}{\text{vol}_b \times d_w} = \frac{50}{20 \times 1} = 2.5 \text{ gm/cc}$$

(14)

$$m = 10 \text{ gm} ; \quad \text{vol} = 20 \text{ cm}^3 ; \quad d_w = 1 \text{ gm/cc}$$

$$\text{Relative density} = \frac{m_b}{\text{vol}_b \times d_w} = \frac{10}{20 \times 1} = \frac{1}{2} = 0.5$$

(15)

$$d = 50 \text{ kg/m}^3 ; \quad \text{volume} = 5 \text{ m}^3$$

$$\text{mass} = d \times \text{vol} = 50 \times 5 = 250 \text{ kg}$$

(16)

$$m = 20 \text{ kg} ; \quad d = 10 \text{ m}^3 \quad \text{density} = \frac{m}{V} = \frac{20}{10} = 2 \text{ kg/m}^3$$

(17)

$$m = 1 \text{ kg} ; \quad d = 2 \text{ kg/m}^3 \quad \text{volume} = \frac{m}{\text{den}} = \frac{1}{2} = 0.5$$
$$= 5 \times 10^{-1} \text{ m}^3$$