

①

Tank

①

Given No. of steps  $N = 40$

width  $w = 35 \text{ cm}$ ; height  $h = 25 \text{ cm} = 25 \times 10^{-2} \text{ m}$

mass  $m = 20 \text{ kg}$ ; Total height to which he ascends  $= nh$

work done  $= mgh$

$= nmgh$

$$= 40 \times 20 \times 10 \times 25 \times 10^{-2}$$

$$= 40 \times 50 = 2000 = 2 \times 10^3 \text{ J}$$

②

Given mass  $m$  rain drop  $= \frac{1}{10} \text{ gm} = \frac{1}{10} \times 10^{-3} = 10^{-2} \text{ kg}$

displacement  $s = 100 \text{ m} = \text{height from which it falls}$

$\therefore$  work done by gravity  $w = mgh$

$$\Rightarrow w = 10^{-2} \times 9.8 \times 100 = 9.8 \text{ J}$$

③

Acceleration of bucket  $a = \frac{g}{4}$

displacement of bucket  $s = d$

work done  $= F \times \text{displacement}$

$$= m(g-a)d$$

$$= m\left(g - \frac{g}{4}\right)d$$

$$\text{or } w = \frac{3}{4}mgd$$

(4)

Given

mass  $m = 5 \text{ kg}$  : initial speed  $u = 0$ Force  $F = 2 \text{ N}$  , time  $t = 10 \text{ sec}$ 

$$\text{Acceleration } a = \frac{F}{m} = \frac{2}{5}$$

$$\text{displacement } s = ut + \frac{1}{2}at^2$$

$$\Rightarrow s = 0 \times 10 + \frac{1}{2} \times \frac{2}{5} \times 10^2$$

$$\Rightarrow s = 0 + \frac{1}{5} \times 100 = 20 \text{ m}$$

$$\text{work done by the force } W = F \cdot s = 2 \times 20 = 40 \text{ J}$$

(5)

Given

$$\frac{m_1}{m_2} = \frac{1}{2} ; \frac{S_1}{S_2} = \frac{2}{1} ; \frac{F_1}{F_2} = \frac{1}{2} \quad \theta_1 = 30^\circ \quad \theta_2 = 60^\circ$$

we know

$$W = F S \cos \theta$$

$$\Rightarrow \frac{W_1}{W_2} = \frac{F_1}{F_2} \times \frac{S_1}{S_2} \times \frac{\cos \theta_1}{\cos \theta_2}$$

$$\Rightarrow \frac{W_1}{W_2} = \frac{1}{2} \times \frac{2}{1} \times \frac{\cos 30^\circ}{\cos 60^\circ} = \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}} = \frac{\sqrt{3}}{1}$$

(6)

Given

 $\frac{1}{5}$ th part of chain is hanging from the table.If  $\frac{1}{n}$ th part is hanging, the amount of work done to

$$\text{left hanging part is } W = \frac{mgL}{2n^2} = \frac{mgL}{2(5)^2} = \frac{mgL}{50}$$

(7)

Given  $m = 10 \text{ kg}$ 

$$\text{work done} = \text{Area of graph} \times m$$

$$= \frac{1}{2} \times b \times h \times m$$

$$\Rightarrow W = \frac{1}{2} \times 8 \times 20 \times 10 \times 10^{-2} \times 10^3$$

$$= 8 \times 10^2 \text{ J}$$

$$[W = F \cdot s = m \cdot a \cdot s \quad \text{Area of graph}]$$

(11)

Task Advanced level

Direction of friction and displacement are in opposite direction.

$$W = F s \cos \theta \quad (\theta = 180^\circ)$$

$$W = F s \cos 180^\circ = -F s = -W$$

For a vertically projected body gravitational force displacement are opposite

$$W = F_g s \cos \theta \quad [\theta = 180^\circ]$$

$$W = F_g s \cos 180^\circ = -F_g s = -W$$

(12)

Given mass = m

$$F_g = mg; \text{ height} = h.$$

work =  $mgh$  [Because gravity and displacement are in opp direction]

$$\theta = 180^\circ; \cos 180^\circ = -1$$

work done by applied force

$$W_{\text{app}} = F s \cos \theta \quad [\theta = 0^\circ]$$

$$= mgh \cos 0^\circ = mgh$$

$$\therefore W_{\text{total}} = -mgh + mgh = 0$$

(13)

(a) centripetal force and displacement are perpendicular to each other  $\theta = 90^\circ$

$$W = F_c s \cos \theta = F s \cos 90^\circ = 0$$

(b)

Tension and displacement are perpendicular to each other  $\theta = 90^\circ$

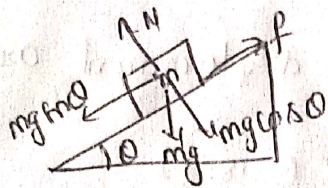
$$W = T s \cos \theta = T s \cos 90^\circ = 0$$

(c)

when a carrying load on his head and standing at a place.  $W = 0$  [displacement  $s = 0$ ]

$$W = F s = F(0) = 0 \text{ J}$$

(14)



$$\text{work done} = \text{Force} \times \text{displacement} \cos \theta$$

$$= (mg \sin \theta) s$$

work done by frictional force is -ve.

work done by gravity  $\cos 0 = 0$ .

(16)

$$\text{Since work done} = F s \cos \theta$$

Displacement is zero for round trip.

There is a centripetal force acting on the body.

(17)

A man pushes wall and fails to displace it. The wall exerts a force on man and displaces him.

$$\text{work done by wall on man} = F s \cos \theta$$

$$= F s \cos 180^\circ$$

$$= -F s$$

// END //

(19)

Given  $m = 300 \text{ kg}$ ; initial speed  $u = 0$ ;  $v = 90 \text{ kmph} = 25 \text{ m/s}$

Time  $= 5 \text{ sec}$ ; displacement  $= 105 \text{ km} = 1.05 \times 10^3 \text{ m}$

$$\text{From } v = u + at$$

$$25 = 0 + a \times 5$$

$$a = 5 \text{ m/s}^2$$

$$\text{Force} = m a = 300 \times 5 = 1500 \text{ N}$$

$$\text{work done} = F s = 1500 \times 1.05 \times 10^3$$

$$= 1575 \times 10^3 \text{ J}$$

## LTank CUGH

(1)

we know work done  $W = FS \cos \theta$  it means that work done depends on force ( $F$ ), displacement ( $S$ ) and angle between  $F$  &  $S$  so it is independent on time.

work done by a force is dependent on the frame of reference.

For ex<sup>o</sup> - if an object is falling under ~~up~~ gravity, there will be a  $G = F$  acting on the object such that it is constant whether we are moving in a frame of reference along with the falling object or whether we are stationary w.r.t ground.

(2)

we know  $\text{Power} = \frac{W}{t}$  so slope of  $W$ -time given power

(3)

work done in lifting the box from ground =  $mgh$   
here  $mg \rightarrow$  weight of the box.

(4)

when a body projected vertically upwards force and displacement are opposite to each other [ $\theta = 180^\circ$ ] so it follows a straightline path.

(4)

(6), (7)

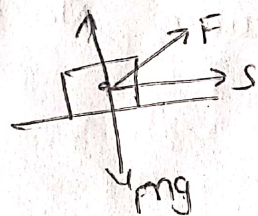
we know  $w = FS \cos \theta$ if force and displacement are perpendicular  $\{\theta = 90^\circ\}$ 

$$w = FS \cos 90^\circ = FS(0) = 0 \text{ J.}$$

if both force and displacement are in same direction  $\theta = 0^\circ$   $w = FS \cos 0^\circ = \underline{FS}$

(9)

when a body is pulled on level surface



Gr.  $F(mg)$  and  $\vec{S}$  are in perpendicular direction  $\theta = 90^\circ$   $w = mgS \cos 90^\circ$   
 $w = 0$

(10)

we know that  $w = FS \cos \theta$ 
 $w = mgS \cos \theta$  clearly work done

is independent on velocity of the body.

(8)

The force acts on body to displace, it moves through a certain distance.

it experiences an increase in energy through a mechanical influence.

## See main level

①

Given force  $F = 50 \text{ N}$  : displacement  $s = 5 \text{ m}$

$$\text{work done} = F s \Rightarrow 50 \times 5 = 250 \text{ J}$$

②

Given force  $= 3 \text{ N}$  : displacement  $s = 30 \text{ m}$

$$\text{work done} = F s = 3 \times 30 = 90 \text{ J}$$

③

work done by a man by holding a box on his head is zero because no displacement.

④

No. of cement bags  $N = 4$

mass  $m = 50$  : height  $h = 20 \text{ m}$

$$\text{work done} = N m g h$$

$$= 4 \times 50 \times 10 \times 20$$

$$\Rightarrow 4 \times 10^4 \text{ J} = 40 \text{ kJ}$$

we take  $g = 9.8 \text{ m/s}^2$

we will get  $w = 39.2 \text{ kJ}$

⑤

Given  $m = 60 \text{ kg}$  : displacement  $s = 30 \text{ m}$  : Force  $(F) = 3 \text{ N}$

$\theta = 60^\circ$

$$\text{work done} = F s \cos \theta$$

$$\Rightarrow 3(30) \cos 60^\circ$$

$$\Rightarrow 90 \times \frac{1}{2}$$

$$\Rightarrow 45 \text{ J}$$

(5)

(6)

Given  $F = 5\hat{i} - 3\hat{j} + 2\hat{k}$  N

$\vec{r}_1 = 2\hat{i} + 7\hat{j} + 4\hat{k}$  ;  $\vec{r}_2 = 5\hat{i} + 2\hat{j} + 8\hat{k}$

$\therefore$  displacement  $\vec{s} = \vec{r}_2 - \vec{r}_1 = 5\hat{i} + 2\hat{j} + 8\hat{k} - 2\hat{i} - 7\hat{j} - 4\hat{k}$   
 $\vec{s} = 3\hat{i} - 5\hat{j} + 4\hat{k}$

work done =  $\vec{F} \cdot \vec{s} = (5\hat{i} - 3\hat{j} + 2\hat{k}) \cdot (3\hat{i} - 5\hat{j} + 4\hat{k})$

$\Rightarrow 5 \times 3 + (-3)(-5) + 2(4)$

$\Rightarrow 15 + 15 + 8 = 38 \text{ J}$

(7)

Force  $F = 2\hat{i} + 4\hat{j} + 3\hat{k}$  N.

it is constrained to move along z-axis by 6m

$\therefore s_z = 6 \hat{k} \text{ m}$

work done =  $\vec{F} \cdot \vec{s} = (2\hat{i} + 4\hat{j} + 3\hat{k}) \cdot 6\hat{k}$   
 $= 3 \cdot 6 = 18 \text{ J}$

(8)

initial speed  $u=0$  , mass  $m=20 \text{ kg}$

Force  $F=5 \text{ N}$  ; time  $t=1 \text{ sec}$

From  $F=ma$   $\Rightarrow a = \frac{F}{m} = \frac{5}{20} = \frac{1}{4} \text{ m/s}^2$

From  $s = ut + \frac{1}{2}at^2 \Rightarrow s = 0 \times 1 + \frac{1}{2} \times \frac{1}{4} (1)^2$   
 $s = \frac{1}{8} \text{ m}$

$\therefore$  work done =  $F \cdot s = 5 \times \frac{1}{8} = \frac{5}{8} \text{ J}$

9

Given displacement  $\vec{s} = 10\text{m}$  ; Force  $F = 5\text{N}$ .

work  $w = 25\text{J}$

$$w = FS \cos \theta$$

$$\Rightarrow 25 = 5 \times 10 \times \cos \theta$$

$$\Rightarrow \cos \theta = \frac{25}{50} = \frac{1}{2} \Rightarrow \theta = 60^\circ$$

10

Given Force  $F = 6\hat{i} - 8\hat{j} \text{ N}$ .

displacement  $\vec{s} = 4\hat{i} + 6\hat{j}$ .

work done  $w = \vec{F} \cdot \vec{s} = (6\hat{i} - 8\hat{j}) \cdot (4\hat{i} + 6\hat{j})$

$$w = 6 \times 4 + (-8) \times 6 = 24 + 48 = 72\text{J}$$

Advanced level

2

work done by the gravitational force is -ve because Force and displacement are in opposite directions

$$\theta = 180^\circ \therefore w = FS \cos 180^\circ = -FS.$$

work done by the applied force is +ve because  $F_{\text{applied}}$  and displacement are in same direction.

3, 9, 10

Given  $m = 1\text{kg}$  ; horizontal distance  $s_x = 1\text{m}$ , Force = 8  
vertical distance  $s_y = 2\text{m}$ .

$$w_{\text{Horizontally}} = F_x s_x = 8 \times 1 = 8\text{J}$$

$$w_{\text{vertically}} = m g s_y = m g h = 1 \times 10 \times 2 = 20\text{J}$$

$$w_{\text{net}} = w_H + w_v = 8\text{J} + 20\text{J} = 28\text{J}$$