

WS-1. Area and Volume

Task

① Given Area of a rectangle = 0.7 hectares
 $= 0.7 \times 10^4 \text{ m}^2$

Given one side let it be $b = 60 \text{ m}$.

$\therefore$ From Area. = $l \times b$

$$\Rightarrow 7 \times 10^3 = 60 \times l \Rightarrow l = \frac{7 \times 10^3}{6} = 1.166 \times 10^3 \\ \approx 1167 \text{ m}$$

② we know that area = (side)²

if side is triple then area = (3 side)²
 $= 9 (\text{side})^2$

so area becomes 9 times that of original area.

③ we know that area = (side)²

if side is decreased to $\frac{1}{4}$ th then - area = $\left(\frac{1}{4} \text{side}\right)^2$
 $= \frac{1}{16} (\text{side})^2$

so area decreases to $\frac{1}{16}$ th of original value.

④ $1 \text{ dm} = 10^{-1} \text{ m} = 0.1 \text{ m}$.

Given side of a square = $4 \text{ m } 8 \text{ dm} = 4 \text{ m} + 8(0.1)$
 $= 4.8 \text{ m}$

Then area = (Side)² = $(4.8)^2$
 $= 23.04 \text{ m}^2$

⑤ Given length $l = 40 \text{ cm}$; breadth $b = 15 \text{ m}$

Then area = $l \times b = 40 \times 15 \Rightarrow 600 \text{ cm}^2$
 $= 6 \text{ m}^2$



⑥ Given length $l = 12 \text{ cm}$; $b = 9 \text{ cm}$; $h = 5 \text{ cm}$

Then the volume of a cuboid $= l \times b \times h$
 $= 12 \times 9 \times 5$
 $= 540 \text{ cm}^3$

⑦ Given $l = 30 \text{ cm}$; $b = 10 \text{ cm}$; $h = 5 \text{ cm}$

Then the volume of the book $V = l \times b \times h$
 $= 30 \times 10 \times 5$
 $= 1500 \text{ cm}^3$

⑧ water level in a given cylinder $V_1 = 16.5 \text{ ml}$
 $V_2 = 23 \text{ ml}$

water level + stone

$\therefore$ Volume of the stone $= V_2 - V_1$
 $= 23 - 16.5 = 6.5 \text{ ml}$

⑨ water level in a cylinder $V_1 = 23 \text{ ml}$
 water level with stone $V_2 = 60 \text{ ml}$

$\therefore$ Volume of the stone $= V_2 - V_1 = 60 - 23$
 $= 37 \text{ ml}$

⑩ A cube has side length $l = 1.6 \times 10^{-2} \text{ m}$

$\therefore$ Volume of the cube $= (\text{side})^3$
 $= (1.6 \times 10^{-2})^3$
 $= (16 \times 10^{-3})^3$
 $= 4096 \times 10^{-9}$

$= 4.096 \text{ m}^3$

⑪ a) $s = 8 \text{ cm} \rightarrow \text{area} = s^2 = 8^2 = 64 \text{ cm}^2$

b) $s = 16 \text{ cm} \rightarrow \text{area} = s^2 = 16^2 = 256 \text{ cm}^2$

c) $s = 5 \text{ cm} \rightarrow \text{Area} = s^2 = 5^2 = 25 \text{ cm}^2$

d) $s = 3 \text{ cm} \rightarrow \text{Area} = s^2 = 3^2 = 9 \text{ cm}^2$

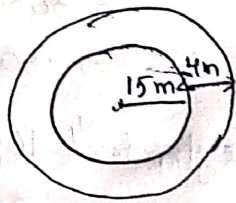
16. level of water in a cylinder $V_1 = 22.5 \text{ ml}$

level of water with stone is $V_2 = 41.0 \text{ ml}$

(i) The increase in water level = $V_2 - V_1 = 18.5 \text{ ml}$

(ii) Volume of stone = $V_2 - V_1 = 18.5 \text{ ml}$

(17)



$\therefore$ Radius of the Park = $15 + 4 = 19 \text{ m}$

$\therefore$ Area of the Park = πr^2

$$= 3.14 \times (19)^2$$

$$= 1133.54 \text{ m}^2$$

(18)

Given the volume of a cuboid = 5400 m^3 .

length $l = 30 \text{ m}$, breadth $b = 20 \text{ m}$ then

$h = ?$

According to the volume of a cuboid

$$V = l \times b \times h$$

$$\Rightarrow 5400 = 30 \times 20 \times h \Rightarrow h = 9 \text{ m}$$

(19)

Given Volume of a cylinder = Area of a sphere

$$\Rightarrow \pi r^2 h = \frac{4\pi}{3} r^3$$

$$\Rightarrow h = \frac{4}{3} r \Rightarrow h = \frac{4}{3} \times 3$$

$$\Rightarrow h = 4 \text{ m.}$$

[Here radius of cylinder = radius of sphere = 3 m]

(20)

Given $l = 180 \text{ cm}$; width = 90 cm

Area of the Paper $A = l \times w = 180 \times 90 \text{ cm}^2$

They gave dimensions (l, w) of envelopes as $10 \text{ cm} \times 4 \text{ cm}$

So area of envelope $a = 10 \text{ cm} \times 4 \text{ cm}$

$\therefore$ No. of envelopes made with Paper = $\frac{\text{Area of Paper}}{\text{Area of Each envelope}}$

$$N = \frac{180 \times 90}{10 \times 4} = 405$$

LTASK SQA's

- ① Volume of oil in a pot $V = 2.85 \text{ m}^3$
capacity of each bottle $V = 300 \text{ ml}$
 $1 \text{ ml} = 10^{-3} \text{ m}^3$

$$\text{No. of bottles } N = \frac{\text{volume of oil}}{\text{capacity of each bottle}}$$

$$N = \frac{2.85}{300 \times 10^{-3}} = \frac{2850}{300} = 9.5 \times 10^3$$

$$N = 9500$$

② unit of volume = cm^3 (or) m^3

unit of area = cm^2 (or) m^2

$$\therefore \frac{\text{unit of volume}}{\text{unit of area}} = \frac{\text{cm}^3}{\text{cm}^2} \text{ (or) } \frac{\text{m}^3}{\text{m}^2}$$
$$= \text{cm (or) m which is}$$

the unit of length.

③ Given side length = $1.5 \times 10^{-2} \text{ m}$

$$\therefore \text{volume of cube} = (\text{side length})^3 = (1.5 \times 10^{-2})^3$$

$$= (1.5 \times 10^{-2})^3 = 15^3 \times 10^{-6}$$

$$= 3.375 \times 10^{-6} \text{ m}^3$$

④ volume of stone $V_1 = 40 \text{ cm}^3$

volume of water $V_2 = 100 \text{ cm}^3$

After stone was dropped in water, the level of water rises and becomes = $V_1 + V_2$

$$= 40 + 100$$

$$= 140 \text{ cm}^3$$

⑤ Given radius $r = 7\text{ m}$

volume of sphere $V = \frac{4\pi}{3} r^3$

$$= \frac{4}{3} \times \frac{22}{7} \times (7)^3$$

$$\Rightarrow \frac{88}{3} \times 7^2 = \frac{88}{3} \times 49$$

$$= 1436\text{ m}^3$$

⑥ Given Area $A = 225\text{ m}^2$

Area of a square $= 225\text{ m}^2$

$$\Rightarrow (\text{side})^2 = (15)^2$$

$$\Rightarrow \text{side} = 15\text{ m}$$

⑦ Given base $= 6\text{ m}$; height $= 10\text{ m}$

Then area of a triangle $= \frac{1}{2} \times \text{base} \times \text{height}$

$$= \frac{1}{2} \times 6\text{ m} \times 10\text{ m}$$

$$= 30\text{ m}^2$$

⑧ Given area of a cylinder $= 81\text{ m}^2$; height $= 1\text{ m}$

$$\pi r^2 h = 81$$

$$\Rightarrow 3.14 \times r^2 \times 1 = 81$$

$$\Rightarrow r^2 = \frac{81}{3.14} \Rightarrow r = 5.07\text{ m}$$

⑨ Given $r = 5\text{ m}$

Area of sphere $= 4\pi r^2$

$$= 4 \times 3.14 \times 5^2$$

$$\Rightarrow 100 \times 3.14$$

$$= 314\text{ m}^2$$



(10) breadth = 4 m. $l = 3b = 3 \times 4$
 $l = 12 \text{ m.}$

$\therefore$ Area of rectangle = $l \times b$
 $= 4 \times 12$
 $= 48 \text{ m}^2$

(16) volume of med. Tonic $V_1 = 480 \text{ ml}$
 capacity of each spoon = 4 ml.

(i) Volume of tonic consumed by David
 per day $V_2 = 3 \text{ spoons}$
 $= 3 \times 4 \text{ ml}$
 $V_2 = 12 \text{ ml.}$

(ii) No. of days that David had taken

Tonic = $N = \frac{\text{volume of Tonic } V_1}{V_2}$

$N = \frac{480}{12} = 40 \text{ days.}$

(iii) $4 \text{ ml} = 4 \times 10^{-3} \text{ lit}$

(17) length of reading room = 6 m

breadth = 6.5 m.

$\therefore$ Area of reading room = $l \times b = 6 \times 6.5 = 39 \text{ m}^2$

(18) Given For reading table $l = 2.5$

Area = 8.5 m^2

$\Rightarrow b \times l = 8.5 \text{ m}^2$

$\Rightarrow b \times 2.5 = 8.5$ 3.4 m

$b = 3.4 \text{ m}$

(19) For Geometry box

$l = 0.42 \text{ m}$; $b = 0.15 \text{ m}$; Area = $l \times b$

$= 0.42 \times 0.15$

$= 0.063 \text{ m}^2$

Q1 Given volume of sphere $V = 1889 \text{ m}^3$

$$\Rightarrow \frac{4\pi}{3} r^3 = 1889$$

$$\Rightarrow \frac{4 \times 3.14}{3} r^3 = 1889$$

$$\Rightarrow r^3 = (7.66 \text{ m})^3$$

$$\Rightarrow r = 7.66 \text{ m}$$

Q2 Given Area of triangle $= 40 \text{ m}^2$; base $= 10 \text{ m}$

$$\Rightarrow \frac{1}{2} \times \text{base} \times \text{height} = 40 \text{ m}^2$$

$$\Rightarrow \frac{1}{2} \times 10 \times h = 40$$

$$\Rightarrow h = 8 \text{ m}$$