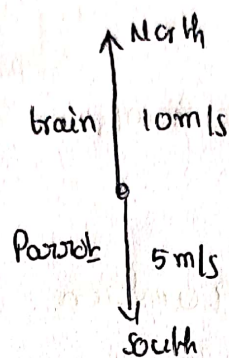


Thank.

①

Direction of motion of train = 10 m/s towards north



$\hat{j}, -\hat{j}$ are unit vectors along North and South.

$\therefore$ The Relative velocity of Parrot with respect to train

$$V_{PG} = -5 \hat{j} \text{ m/s}$$

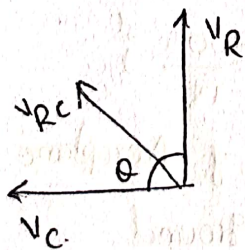
$$\begin{aligned} V_{PE} &= V_{PG} + V_{EG} \\ &= +5 \hat{j} + 10 \hat{j} \\ &= 15 \hat{j} \end{aligned}$$

$$\Rightarrow |\vec{V}_{PE}| = 15 \text{ m/s.}$$

$$\therefore \text{Time taken} = \frac{\text{distance}}{\text{velocity}}$$

$$= \frac{150}{15} = 10 \text{ sec.}$$

②



Here $V_R \rightarrow$ Velocity of rocket

$V_C \rightarrow$ Velocity of Car = 6 m/s

$V_{RC} \rightarrow$ velocity of rocket with respect to Car driver. = 10 m/s

$$\text{we know that } V_{RC} = \sqrt{V_R^2 + V_C^2 + 2V_R V_C \cos \theta} \quad [\text{Here } \theta = 90^\circ]$$

$$\Rightarrow V_{RC} = \sqrt{V_R^2 + V_C^2 + 2V_R V_C \cos 90}$$

$$\Rightarrow V_{RC} = \sqrt{V_R^2 + V_C^2}$$

$$\Rightarrow 10 = \sqrt{V_R^2 + 6^2}$$

on squaring both sides we get

$$10^2 = 6^2 + v_R^2$$

$$\Rightarrow 100 = 36 + v_R^2$$

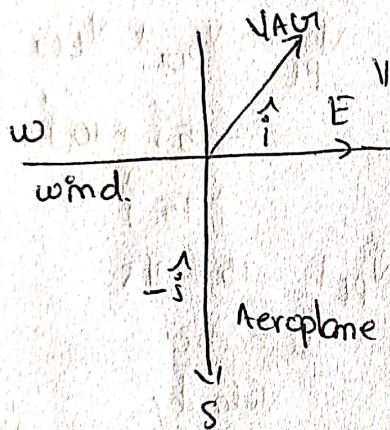
$$\Rightarrow 100 - 36 = v_R^2$$

$$\Rightarrow v_R^2 = 64$$

$$\Rightarrow v_R = \sqrt{64} = 8 \text{ m/s}$$

③

According to given question



$V_{Aw} = V_{Aa}$ = velocity of aeroplane with respect to air = 800 kmph

$$= 800 \times \frac{5}{18}$$

$$= \frac{4000}{18} \text{ m/s}$$

$$V_{wind} = 15 \text{ m/s}$$

$$V_{AG} = 15 \hat{j} \text{ m/s}$$

$$V_{Aw} = \text{vel } V_{AG} - V_{wG}$$

$$\Rightarrow -\frac{4000}{18} \hat{j} = -15 \hat{i} + V_{AG}$$

$$\Rightarrow V_{AG} = 15 \hat{i} + \frac{4000}{18} \hat{j}$$

$\therefore |V_{AG}|$ = Magnitude of Velocity of Aeroplane with respect to ground

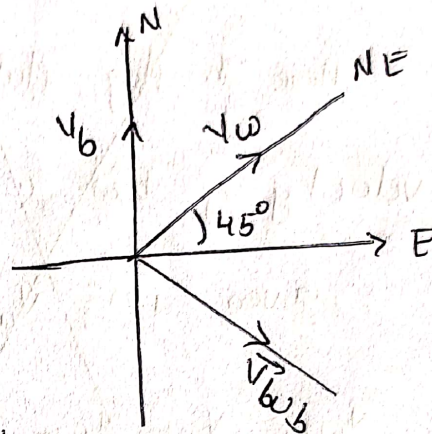
$$= \sqrt{(15)^2 + \left(\frac{4000}{18}\right)^2}$$

$$= \sqrt{225 + 49,372} = \sqrt{49,597}$$

$$= 222.7 \text{ m/s}$$

(k)

Since the flag flutters in a boat in NE direction we could conclude that the velocity of wind is in NE direction



when the boat sail towards north $= V_B = 51 \hat{j}$ kmph

The flag would flutter along the direction of relative velocity with respect to wind boat.

Velocity of Flag $V_F = V_w = 72$ kmph in NE

$$\therefore \vec{V}_{WB} = \vec{V}_w - \vec{V}_B = 72 \cos 45^\circ \hat{i} + 72 \sin 45^\circ \hat{j}$$

Here $\theta = 45^\circ$

$$\Rightarrow [72 \cos 45^\circ \hat{i} + 72 \sin 45^\circ \hat{j}] - 51 \hat{j}$$

$$\Rightarrow \frac{72}{\sqrt{2}} \hat{i} + \frac{72}{\sqrt{2}} \hat{j} - 51 \hat{j}$$

$$\Rightarrow 50.91 \hat{i} + (50.91 - 51) \hat{j}$$

$$\Rightarrow 50.91 \hat{i} - 0.09 \hat{j}$$

Angle made by the vector $\vec{V}_{WB}$ with x-axis is

$$\tan \alpha = \frac{y\text{-component}}{x\text{-component}} = \frac{-0.09}{50.91}$$

$$\alpha = 0.1^\circ \text{ with x-axis (i.e.) with East}$$

$\therefore$ Direction of fluttering of Flag is almost towards east

(3)

(5)

Given wind is flowing from south. i.e. it is flowing towards north $\therefore \vec{V}_{WG} = 10\hat{j}$ m/s

But to the cyclist it appears to blow from the east at 10 m/s

so velocity of wind relative to the cyclist is 10 m/s from east to west.

$$\vec{V}_{WC} = -10\hat{i}$$

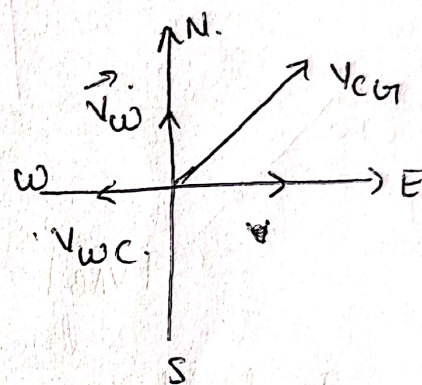
$$\Rightarrow \vec{V}_{WG} - \vec{V}_{CG} = -10\hat{i}$$

$$\Rightarrow \vec{V}_{CG} = \vec{V}_{WG} + 10\hat{i}$$

$$\vec{V}_{CG} = 10\hat{j} + 10\hat{i}$$

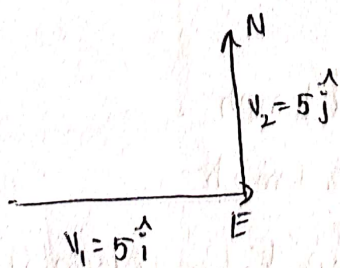
$$\therefore |\vec{V}_{CG}| = \sqrt{10^2 + 10^2} = 10\sqrt{2} \text{ m/s}$$

Here $\hat{i}, \hat{j}$ are unit vectors along east & north directions.



(6)

According to given question



$$\therefore \text{velocity of the particle} = v_1\hat{i} + v_2\hat{j} = 5\hat{i} + 5\hat{j}$$

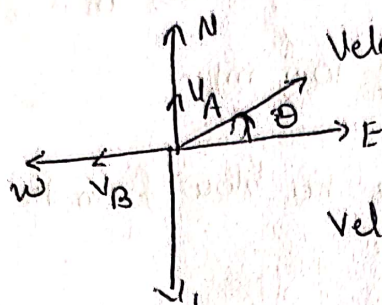
$$\Rightarrow |\vec{V}| = \sqrt{5^2 + 5^2} = 5\sqrt{2} \text{ m/s}$$

$$\text{time of change } t = 10 \text{ sec}$$

$$\therefore \text{Acceleration } a = \frac{|\vec{V}|}{t} = \frac{5\sqrt{2}}{10} = \frac{\sqrt{2}}{2} = \frac{1}{\sqrt{2}} \text{ NE}$$

⑦

According to given data



Velocity of A = 8 kmph towards north
 $= 8\hat{j}$ kmph

Velocity of B = 6 kmph towards west
 $= 6(-\hat{i})$ kmph

$\therefore$ velocity of A with respect to B

$$\vec{V}_{AB} = \vec{V}_A - \vec{V}_B$$

$$= 8\hat{j} - 6(-\hat{i})$$

$$\vec{V}_{AB} = 8\hat{j} + 6\hat{i}$$

$$\therefore |\vec{V}_{AB}| = \sqrt{8^2 + 6^2} = \sqrt{64 + 36} = \sqrt{100} = 10 \text{ kmph}$$

The direction of $\vec{V}_{AB}$ with x-axis (or) East is

$$\tan \theta = \frac{\text{y-component}}{\text{x-component}}$$

$$\therefore \tan \theta = \frac{8}{6} = \frac{4}{3}$$

$$\therefore \theta = \tan^{-1}\left(\frac{4}{3}\right) \text{ North of East.}$$

⑧

Velocity of rain $V_R = 4$ kmph

velocity of person $V_P = 3$ kmph

Velocity of rain with respect to person $V_{RP} = \sqrt{V_R^2 + V_P^2}$

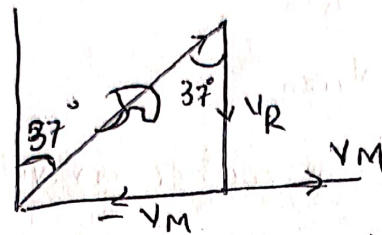
$$\therefore V_{RP} = \sqrt{4^2 + 3^2}$$

$$= \sqrt{16 + 9} = \sqrt{25}$$

$$V_{RP} = 5 \text{ kmph}$$

(9)

Velocity of a man in a car



$$V_M = 10.8 \text{ kmph}$$

$$= \frac{10.8}{18} \times \frac{5}{18}$$

$$= 3 \text{ m/s}$$

Always the umbrella should be hold in a direction of relative velocity of rain with respect to man.

From Fig $\tan 37^\circ = \frac{V_M}{V_R}$

$$\Rightarrow \frac{3}{4} = \frac{3}{V_R}$$

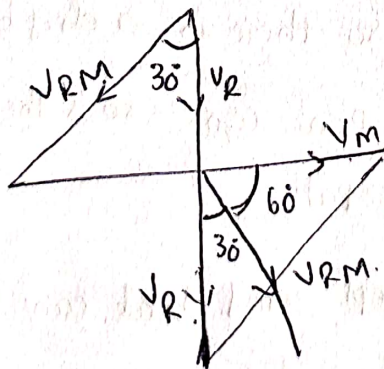
$$\Rightarrow V_R = 4$$

(10)

Given velocity of man = 4 m/s

He finds that rain is falling slant wise into his face $\rightarrow$ this is the Relative velocity of rain with respect to him.

$$V_{RM} = 4 \text{ m/s}$$



$$\vec{V}_{RM} = \vec{V}_R + \vec{V}_M$$

$$\Rightarrow \vec{V}_R = \vec{V}_{RM} - \vec{V}_M \quad [\text{Angle b/w } \vec{V}_M \text{ and } \vec{V}_{RM} \text{ is } 60^\circ]$$

$$\Rightarrow |\vec{V}_R| = \sqrt{V_{RM}^2 + V_M^2 - 2V_{RM}V_M \cos 60^\circ}$$

$$= \sqrt{4^2 + 4^2 - 2 \times 4 \times 4 \times \cos 60^\circ}$$

$$= \sqrt{4^2 + 4^2 - 2 \times 4^2 \times \frac{1}{2}} = \sqrt{4^2 + 4^2 - 4^2}$$

$$= \sqrt{4^2} = 4 \text{ m/s}$$

(13)

Given $V_{BW} = n V_{RW}$ (or)

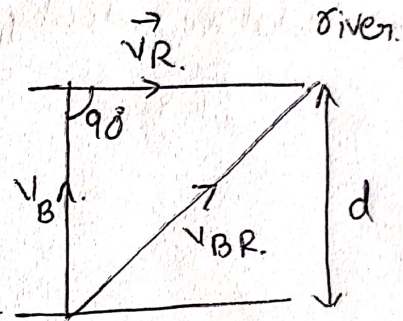
$$V_{BW} = n V_{WR}$$

where V_W = velocity of water (or) velocity of river

V_{BW} = velocity of Boat with respect to water (or)

$$\therefore \vec{V}_{BR} = \vec{V}_{BW} - \vec{V}_{RW}$$

$$\Rightarrow \vec{V}_{BW} = \vec{V}_{BR} + \vec{V}_{RW}$$



$$\Rightarrow |\vec{V}_{BR}| = \sqrt{(\vec{V}_{BW})^2 + (\vec{V}_{RW})^2 - 2 V_{BW} (V_{RW}) \cos 90^\circ}$$

$$\vec{V}_{BR} = \sqrt{V_{BW}^2 + (V_{RW})^2} \Rightarrow V_{BW}^2 = V_{BR}^2 - V_{RW}^2 \rightarrow ①$$

Drift $x = d \cdot \frac{V_{RW}}{V_{BW}} = d \cdot \frac{V_{RW}}{n V_{RW}}$

$$x = \frac{d}{n} \rightarrow ② \quad \text{Here } d \text{ is width of river}$$

(b) For $n=1 \Rightarrow x=d$ so there is a drift.

(c) For $n>1 \Rightarrow x<d$ Boat can cross the river along shortest path

(d) For any value of n [except zero] boat can cross the river

From ① $V_{BW}^2 = (n V_{RW})^2 - V_{RW}^2 = (n^2 - 1) V_{RW}^2$

$\Rightarrow V_{BW} = V_{RW} \sqrt{n^2 - 1}$ For $n>0 : V_{BW}>0$, so the boat can cross the river in shortest path.

(16)

(7)

(6)

(14)

let $x \rightarrow$ be the drift suffered by the boat

$$\Rightarrow x = d \times \frac{v_R}{v_{BR}} \text{ and we know that}$$

$$(a) \quad d = 1000 \text{ m} : v_R = 2 \text{ m/s} ; v_B = 4 \text{ m/s} \quad v_B^2 = v_{BR}^2 - v_R^2$$

$$\Rightarrow v_{BR}^2 = 4^2 + 2^2$$

$$\Rightarrow v_{BR}^2 = v_B^2 + v_R^2$$

$$\Rightarrow v_{BR} = \sqrt{20} = 2\sqrt{5} \text{ m/s}$$

$$\therefore x_1 = 1000 \times \frac{2}{2\sqrt{5}} = \frac{1000}{\sqrt{5}} \text{ m}$$

$$(b) \quad d = 500 \text{ m} ; v_R = 1 ; v_B = 6 \text{ m/s}$$

$$\Rightarrow v_{BR}^2 = 6^2 + 1^2 = 36 + 1 = 37$$

$$\Rightarrow v_{BR} = \sqrt{37}$$

$$\therefore x_2 = 500 \times \frac{1}{\sqrt{37}} \text{ m}$$

$$(c) \quad d = 1000 \text{ m} : v_R = 6 \text{ m/s} ; v_B = 6 \text{ m/s}$$

$$\Rightarrow v_{BR}^2 = 6^2 + 6^2 = 36 + 36 = 72$$

$$\Rightarrow v_{BR} = \sqrt{72} = 6\sqrt{2}$$

$$\therefore x_3 = 1000 \times \frac{6}{6\sqrt{2}} = \frac{1000}{\sqrt{2}} \text{ m}$$

$$\therefore x_3 > x_1 > x_2$$

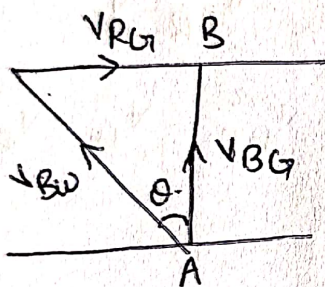
increasing order b, a, c

(15)

velocity of boat in still water $V_{BW} = 5 \text{ kmph}$

width of river $d = 1 \text{ km}$

Time of crossing $t = 15 \text{ min} = \frac{15}{60} \text{ hr}$
 $= \frac{1}{4} \text{ hr}$



$AB = \text{width of river}$

Time taken to cross in shortest path

$$t = \frac{d}{V_{BG}}$$

clearly

$$V_{BG}^2 + V_{RG}^2 = V_{BW}^2$$

$$\Rightarrow V_{BG} = \sqrt{V_{BW}^2 - V_{RG}^2}$$

$$= \sqrt{5^2 - V_{RG}^2}$$

$$\Rightarrow \frac{1}{4} = \frac{1}{\sqrt{5^2 - V_{RG}^2}}$$

$$\Rightarrow \sqrt{5^2 - V_{RG}^2} = 4$$

$$\Rightarrow 5^2 - V_{RG}^2 = 4^2$$

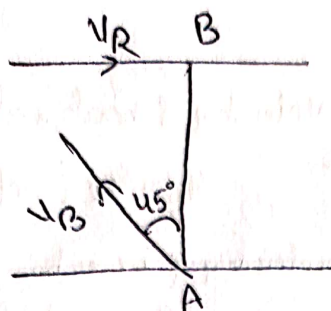
$$\Rightarrow 25 - V_{RG}^2 = 16$$

$$\Rightarrow V_{RG}^2 = 25 - 16$$

$$\Rightarrow V_{RG} = \sqrt{9} = 3 \text{ kmph}$$

V_R R

(16)



A is starting point and B is exactly opposite point

velocity of water = $v_R = v$.

From fig $\sin \theta = \frac{v_R}{v_B}$

$$\Rightarrow \sin 45^\circ = \frac{v}{v_B}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{v}{v_B}$$

$$\Rightarrow v_B = \sqrt{2} v$$

(17)

Velocity of boat with respect to water $\vec{v}_{BW} = 2\hat{i} + 3\hat{j} \text{ m/s}$

velocity of river with respect to ground $\vec{v}_{WG} = 3\hat{i} + 2\hat{j} \text{ m/s}$

$$\therefore \vec{v}_{BW} = \vec{v}_{BG} - \vec{v}_{WG}$$

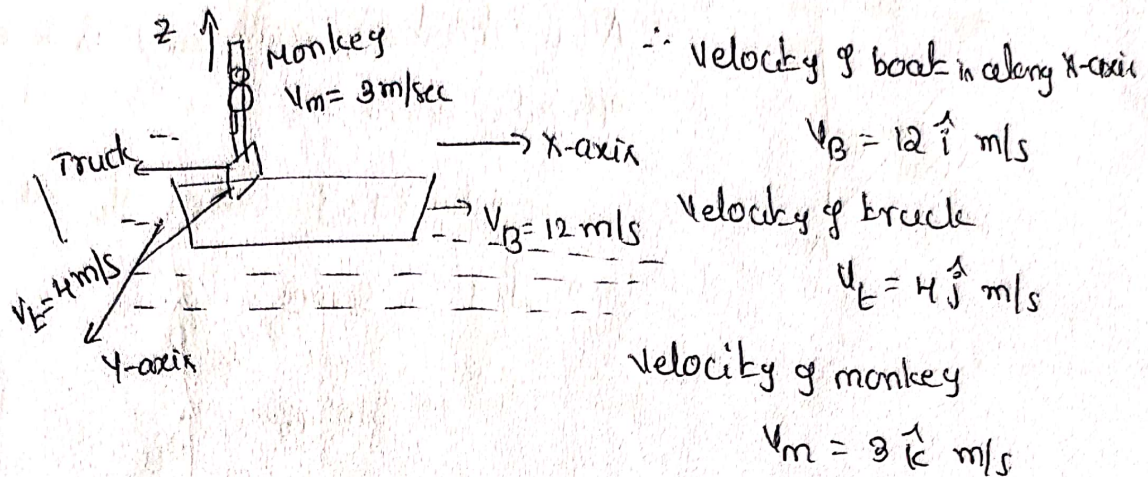
$$\Rightarrow 2\hat{i} + 3\hat{j} = \vec{v}_{BG} - (3\hat{i} + 2\hat{j})$$

$$\Rightarrow 2\hat{i} + 3\hat{j} = \vec{v}_{BG} - 3\hat{i} - 2\hat{j}$$

$$\Rightarrow \vec{v}_{BG} = 2\hat{i} + 3\hat{j} + 3\hat{i} + 2\hat{j}$$

$$\vec{v}_{BG} = 5\hat{i} + 5\hat{j} \text{ m/s}$$

(18)



$\therefore$ velocity of monkey as observed by a man on the shore = Resultant velocity of monkey due to motion of truck & boat

$$\begin{aligned}
 &= v_B + v_E + v_m \\
 &= 12\hat{i} + 4\hat{j} + 3\hat{k} \\
 &= \sqrt{12^2 + 4^2 + 3^2} = \sqrt{144 + 16 + 9} = \sqrt{169} = 13 \text{ m/s}
 \end{aligned}$$

(19)

Let v be the speed of the bus running between town A and B

speed of cyclist $u = 20 \text{ kmph}$

Relative speed of the bus moving in the direction of cyclist = $v - u = (v - 20) \text{ kmph}$

The bus went past the cyclist every $18 \text{ min} = \frac{18}{60} \text{ hr}$

$\therefore$ Distance covered by the bus = speed $\times$ time

$$= (v - 20) \times \frac{18}{60} \rightarrow \text{①}$$

⑦

Since one bus leaves after every T min, then

The distance travelled by the bus will be equal to

$$= V \times \frac{T}{60} \rightarrow (2)$$

Both equations (1) and (2) are equal

$$\therefore (V-20) \times \frac{18}{60} = \frac{V \cdot T}{60}$$

$$\Rightarrow (V-20) \times 18 = \frac{V \cdot T}{60} \rightarrow (3)$$

Relative speed of bus moving in opposite direction of

the cyclist = $(V+20)$ kmph

Time taken by the bus to go past the

$$\text{cyclist} = 6 \text{ min} = \frac{6}{60} \text{ hr} = \frac{1}{10} \text{ hr}$$

The distance travelled by the bus = $(V+20) \times \frac{6}{60} \rightarrow (4)$

$$\Rightarrow \frac{V \cdot T}{60} = (V+20) \frac{6}{60}$$

From (3) and (4)

$$\Rightarrow (V+20) \frac{60}{60} = (V-20) \times \frac{18}{60} \times 3$$

$$\Rightarrow V+20 = 3V-60 \Rightarrow 2V = 80$$

$$\Rightarrow V = 40 \text{ kmph}$$

sub V value in (4) $\frac{40 \times T}{60} = (40+20) \frac{6}{60}$

$$\Rightarrow 40T = 60 \times 6$$

$$\Rightarrow T = \frac{360}{40} = 9 \text{ min}$$

$$T = 9 \text{ min}$$

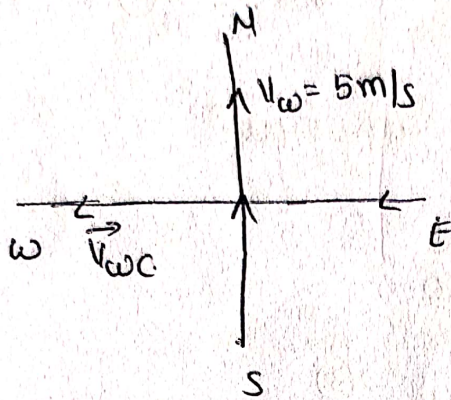


LTask

①

wind is blowing from south to north

$$\text{ie } \vec{v}_{wG} = 5\hat{j} \text{ m/s}$$



To cyclist it appears to blow from west to east to west

(ie) Relative velocity of wind with respect to cyclist is

$$\vec{v}_{wc} = 5(-\hat{i}) \text{ m/s}$$

$$\therefore \vec{v}_{wc} = \vec{v}_{wG} - \vec{v}_{cG}$$

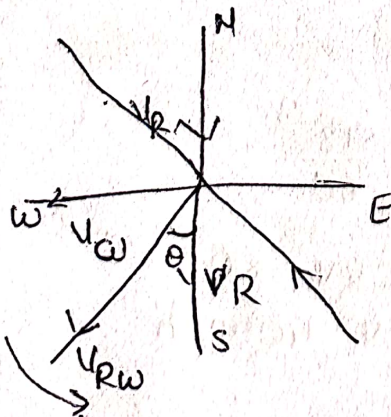
$$\Rightarrow -5\hat{i} = 5\hat{j} - \vec{v}_{cG}$$

$$\Rightarrow \vec{v}_{cG} = 5\hat{j} + 5\hat{i}$$

$$\Rightarrow |\vec{v}_{cG}| = \sqrt{5^2 + 5^2} = 5\sqrt{2} \text{ m/s N-W}$$

②

According to Given question



$$\text{Velocity of Rain } \vec{v}_{Ri} = -30\hat{j} \text{ m/s} \Rightarrow |\vec{v}_{Ri}| = 30 \text{ m/s}$$

$$\text{Velocity of woman } \vec{v}_{wG} = -12\hat{i} \text{ m/s} \Rightarrow |\vec{v}_{wG}| = 12 \text{ m/s}$$

woman has to hold umbrella in the direction opp of Relative velocity ($\vec{v}_{Rw}$)

$$v_{Rw} \text{ From fig } \tan \theta = \frac{v_w}{v_R} = \frac{12}{30}$$

$$\tan \theta = \frac{2}{5}$$

$$\theta = \tan^{-1}\left(\frac{2}{5}\right) \text{ with vertical towards west}$$

(9)

(3)

v_{pw} = velocity of person with respect to water = 5 m/s

v_R or v_w = velocity of river or water = 3 m/s

Time taken for upstream $t_u = \frac{d}{v_{pw} - v_w}$

Time taken for downstream $t_d = \frac{d}{v_{pw} + v_w}$

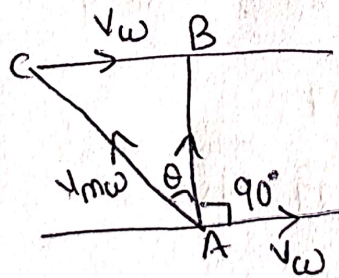
$$\therefore \frac{t_d}{t_u} = \frac{\frac{d}{v_{pw} + v_w}}{\frac{d}{v_{pw} - v_w}} = \frac{v_{pw} - v_w}{v_{pw} + v_w}$$

$$\Rightarrow \frac{t_d}{t_u} = \frac{5-3}{5+3} = \frac{2}{8} = \frac{1}{4}$$

(4)

v_{mw} = velocity of man in still water = 6 kmph

v_w = velocity of river = 3 kmph.



From fig $\sin \theta = \frac{v_w}{v_{mw}}$

$$\Rightarrow \sin \theta = \frac{3}{6} = \frac{1}{2}$$

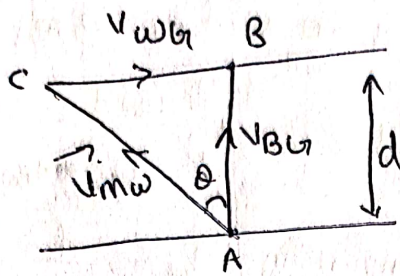
$$\Rightarrow \sin \theta = \frac{1}{2}$$

$$\Rightarrow \theta = 30^\circ$$

$\therefore$ The man has to swim in a direction $(90^\circ + \theta) = 90^\circ + 30^\circ = 120^\circ$ with flow of water.

5

velocity of man in water $V_{mw} = 6 \text{ kmph}$



If the man wants to swim to reach exact opposite point (B) he has to swim along $\vec{AC}$.

Time taken for the boat to cross the river

$$t = \frac{d}{V_{BG}} \rightarrow \textcircled{1}$$

$d = \text{width of river} = 2 \text{ km}$

$V_{wG} = \text{velocity of river w.r. to water} = 3 \text{ kmph}$

From fig $AC^2 = AB^2 + CB^2$

$$\Rightarrow V_{mG}^2 = V_{BG}^2 + V_{wG}^2$$

$$\Rightarrow 6^2 = V_{BG}^2 + 3^2$$

$$\Rightarrow V_{BG}^2 = 6^2 - 3^2 = 36 - 9$$

$$\Rightarrow V_{BG}^2 = 27$$

$$\Rightarrow V_{BG} = \sqrt{27} \text{ m/s}$$

$\therefore$ From $\textcircled{1}$

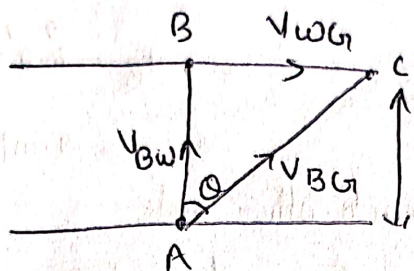
$$t = \frac{2}{\sqrt{27}} \text{ hrs.}$$

(6)

Velocity of water = $V_w = 2 \text{ kmph}$.

width of river = $d = 400 \text{ m}$.

Velocity of boat in still water = $V_{Bw} = 8 \text{ kmph}$.



$BC = \text{drift} = \text{displacement}$

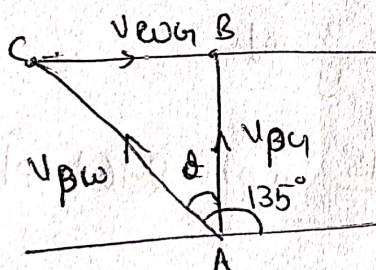
$= \text{velocity} \times \text{time}$

$$= V_w \times \frac{d}{V_{Bw}}$$

$$= 2 \times \frac{400}{8} = 100$$

$$BC = 100 \text{ m}$$

(7)



Given that the Person swims at 135° to current flow

$$\text{i.e. } \theta = 45^\circ$$

$$\text{From fig } \cos \theta = \frac{V_{pw}}{V_w} \quad \text{Given } 135^\circ = \frac{V_p}{V_w}$$

$$\Rightarrow \cos 45^\circ$$

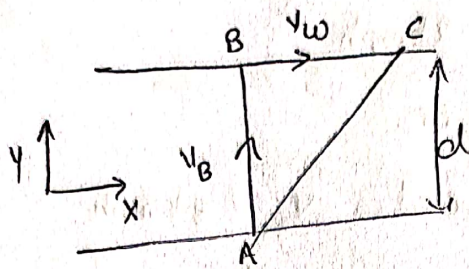
$\Rightarrow$

$$\text{From fig } \sin 135^\circ = \frac{V_w}{V_p}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{V_w}{V_p}$$

$$\Rightarrow \frac{V_p}{V_w} = \frac{1}{\frac{1}{\sqrt{2}}} = \sqrt{2}$$

⑧



$$BC = 150 \text{ m.}$$

width of river $d = 500 \text{ m.}$

Given Velocity of Boat $v_B = 7.2 \text{ kmph}$

$$\Rightarrow v_B = 7.2 \times \frac{5}{18} \text{ m/s}$$

$$= 2 \text{ m/s}$$

Time taken to reach other side

$$t = \frac{sy}{vy} = \frac{d}{v_B} = \frac{500}{2} = 250 \text{ sec.}$$

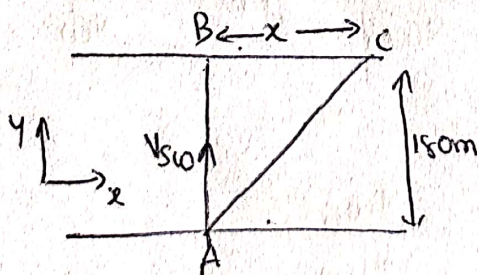
Drift $BC = v_w \times \text{time taken}$

$$\Rightarrow 150 = v_w \times 250$$

$$\Rightarrow v_w = \frac{15}{25} = \frac{3}{5} \text{ m/s}$$

$$= \frac{3}{5} \times \frac{18}{5} \text{ kmph} = 2.16 \text{ kmph}$$

⑨



Velocity of river (or) water $v_w = 0.85 \text{ m/s}$

width of river $d = 180 \text{ m}$

Velocity of swimmer in water $v_{sw} = 1.65 \text{ m/s}$

Time taken to cross river $t = \frac{sy}{vy} \text{ [y-direction]}$

$$\Rightarrow t = \frac{180}{1.65} = 109 \text{ sec.}$$

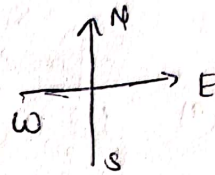
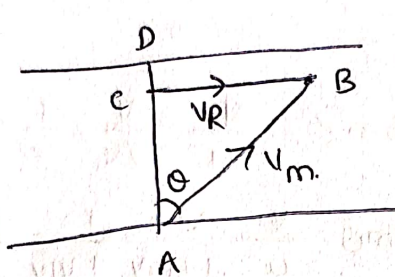
drift $x = v_w \times t$

$$= 0.85 \times 109 \Rightarrow 92.7 \text{ m.}$$

(10)

Given that velocity of river from west to east = 5 m/min

velocity of the person from south bank to the river in still water (V_{man}) = 10 m/min



Here AC is shortest distance for the person to cross the river from the south bank of the river.

The component of velocity of the person along shortest

$$\text{Path} = V_{\text{man}} \cos \theta$$

Now, the time taken by the person to cross the river

along shortest path is given as $t = \frac{AC}{V_{\text{man}} \cos \theta}$

The time will be minimum, when the denominator will be max.

$$\text{i.e. } \cos \theta = \text{maximum}$$

$$\text{Maximum value of } \cos \theta = 1$$

$$\therefore \cos \theta = \cos 0^\circ$$

$$\Rightarrow \theta = 0^\circ \quad \text{that is in the north}$$

direction, thus the direction in which the swimmer should move will be in north direction.

13

U = velocity of boat in still water.

V = velocity of river.

The angle made by the boat with river flow

$$\sin \theta = \frac{V_R}{V_B}$$

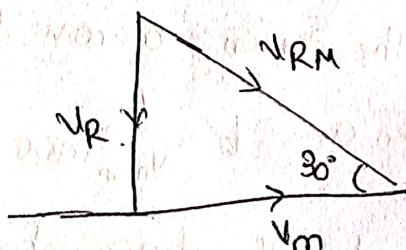
(a) If $U = 2V$ $\Rightarrow \sin \theta = \frac{V}{U} = \frac{V}{2V} = \frac{1}{2} \Rightarrow \theta = 30^\circ$

(b) If $U = 1.414V$ $\Rightarrow \sin \theta = \frac{V}{U} = \frac{V}{1.414V} = \frac{1}{1.414} = \frac{1}{\sqrt{2}} \Rightarrow \theta = 45^\circ$

(c) If $U = V \Rightarrow \sin \theta = \frac{V}{U} = \frac{V}{V} = 1 \Rightarrow \theta = 90^\circ$

15

According to given data

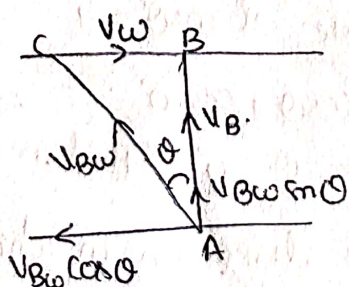


V_m = velocity of river = 5 kmph

From fig $\tan 30^\circ = \frac{V_P}{V_m}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{V_P}{5} \Rightarrow V_P = \frac{5}{\sqrt{3}} = 2.9 \text{ kmph}$$

11



From fig $\sin \theta = \frac{V_w}{V_{BoW}}$

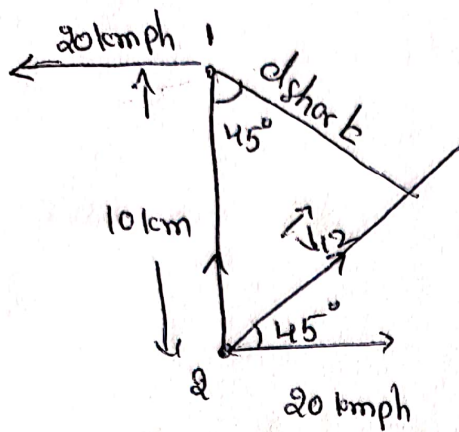
$$\Rightarrow \sin 60 = \frac{V_w}{V_{BoW}} \Rightarrow \frac{\sqrt{3}}{2} = \frac{V_w}{V_{BoW}}$$

From fig $V_{BoW} \cos 60 = V_{Bo}$

$$\Rightarrow V_{BoW} \frac{1}{2} = V_{Bo}$$

$$\Rightarrow V_{BoW} = 2 V_{Bo}$$

(16)



The velocity components of both ships 1 and 2 are equal.

Hence the angle between the

two vectors is 45°

$$\text{From fig } \sin 45^\circ = \frac{d_{\text{short}}}{10 \text{ km}}$$

$$\begin{aligned} \Rightarrow d_{\text{short}} &= 10 \sin 45^\circ \\ &= 10 \times \frac{1}{\sqrt{2}} \\ &= 5\sqrt{2} \text{ km} \end{aligned}$$

Time taken to reach the point [distance of closest approach]

$$t = \frac{d_{\text{short}}}{|\vec{v}_{21}|} = \frac{5\sqrt{2}}{\frac{20\sqrt{2}}{4}} = \frac{1}{4} \text{ hrs} = 15 \text{ min}$$

$$\begin{aligned} \vec{v}_{21} &= \vec{v}_2 - \vec{v}_1 = 20\hat{i} - (-20\hat{i}) \\ &= -20\hat{i} + 20\hat{j} \end{aligned}$$

$$|\vec{v}_{21}| = \sqrt{(20)^2 + (20)^2} = 20\sqrt{2} \text{ kmph}$$