

8. ELIMINATION OF ANGLE

①

2025/26

Class: VIII. MATHEMATICS

FOUNDATION: SOLUTIONS

TEACHING TASK

JEE MAINS

01. short trick method

$$\text{Let } \theta = 45^\circ$$

$$\therefore \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} = p \quad \left| \quad 1+1=2 \right.$$

$$\Rightarrow \boxed{p = \sqrt{2}} \quad \left| \quad \boxed{q = 2} \right.$$

$$\therefore q(p^2 - 1) = 2((\sqrt{2})^2 - 1) = 2(2 - 1) = 2 \quad \text{Ans. B}$$

02 $a - b = \left(\frac{x}{\sqrt{2}} + \frac{y}{\sqrt{2}} \right) - \left(\frac{x}{\sqrt{2}} - \frac{y}{\sqrt{2}} \right)$

$$= \frac{2y}{\sqrt{2}} = \sqrt{2} y$$

Ans: B

03 $\sec \theta = a + \frac{1}{4a}$

$$\Rightarrow 2\sec \theta = 2a + \frac{1}{2a}$$

$$(\sec \theta + \tan \theta) + (\sec \theta - \tan \theta) = 2a + \frac{1}{2a}$$

$$\Rightarrow \sec \theta + \tan \theta = 2a$$

Ans. B

Short trick method

(2)

$$\text{put } \theta = 0^\circ$$

$$m = a \quad | \quad n = 0$$

$$(m+n)^{\frac{2}{3}} + (m-n)^{\frac{2}{3}}$$

$$= (a)^{\frac{2}{3}} + (a-0)^{\frac{2}{3}} = 2 \cdot a^{\frac{2}{3}}$$

Ans: D

$$x^2 + y^2 = a^2 \cos^6 \theta \cdot \sin^4 \theta + a^2 \sin^6 \theta \cdot \cos^4 \theta$$

$$= a^2 \cos^4 \theta \sin^4 \theta (\cos^2 \theta + \sin^2 \theta)$$

$$= a^4 \cos^4 \theta \sin^4 \theta$$

$$xy = (a \cos^3 \theta \cdot \sin^5 \theta)(a \sin^3 \theta \cdot \cos^5 \theta)$$

$$= a^2 \cos^5 \theta \cdot \sin^5 \theta$$

$$\frac{(x^2 + y^2)^p}{(xy)^q} = \frac{(a^4 \cos^4 \theta \cdot \sin^4 \theta)^p}{(a^2 \cos^5 \theta \cdot \sin^5 \theta)^q}$$

$$= a^{4p-2q} \cdot \cos^{4p-5q} \cdot \sin^{4p-5q}$$

This is independent of θ

$$\Rightarrow 4p - 5q = 0$$

$$\Rightarrow 4p = 5q$$

Ans: A

06. Short cut method

(3)

$$x = \cot \theta + \tan \theta, \quad y = \sec \theta - \csc \theta$$

$$\text{let } \theta = 45^\circ \quad \left| \quad y = \sqrt{2} - \frac{1}{\sqrt{2}} \right.$$

$$\Rightarrow x = 1 + 1$$

$$\Rightarrow x = 2$$

$$y = \frac{1}{\sqrt{2}}$$

$$\text{Now, } (x^2 y)^{\frac{2}{3}} - (x y^2)^{\frac{2}{3}}$$

$$= \left(4 \cdot \frac{1}{\sqrt{2}} \right)^{\frac{2}{3}} - \left(2 \cdot \frac{1}{2} \right)^{\frac{2}{3}} = 2 - 1 = 1$$

NOTE:
A.C Both opt

Ans. A.C

$$07 \quad \left. \begin{array}{l} \text{let } \theta = 45^\circ \\ x = a(\sqrt{2} + 1) \end{array} \right\} y = \frac{b(1 - \frac{1}{\sqrt{2}})}{(\frac{1}{\sqrt{2}})} = b(\sqrt{2} - 1)$$

$$\text{Now } xy = ab(\sqrt{2} + 1)(\sqrt{2} - 1) = ab$$

Ans. C

$$08 \quad \begin{array}{l} a \sec \theta + b \tan \theta + c = 0 \rightarrow (1) \\ p \sec \theta + q \tan \theta + r = 0 \rightarrow (2) \end{array}$$

$$(1) \times q \Rightarrow aq \sec \theta + bq \tan \theta + cq = 0$$

$$(2) \times b \Rightarrow bp \sec \theta + bq \tan \theta + br = 0$$

$$\Rightarrow (aq - bp) \sec \theta + (cq - br) = 0$$

$$\Rightarrow \sec \theta = \frac{br - cq}{aq - bp}$$

$$\text{Similarly } \tan \theta = \frac{pc - ar}{aq - bp}$$

Now, $\sec^2 \theta - \tan^2 \theta = 1$

(4)

$$\Rightarrow \left(\frac{br - cq}{aq - bp} \right)^2 - \left(\frac{pc - ar}{aq - bp} \right)^2 = 1$$

$$\Rightarrow (br - cq)^2 - (pc - ar)^2 = (aq - bp)^2 \quad \text{Ans: C}$$

09 $\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = \sec^2 \theta \cdot \cos^2 \phi + \sec^2 \theta \cdot \sin^2 \phi$

$$= \sec^2 \theta (\cos^2 \phi + \sin^2 \phi) - \tan^2 \theta$$

$$= \sec^2 \theta - \tan^2 \theta = 1$$

Ans: A

10 $\left(\frac{x}{a} \right)^2 - \left(\frac{y}{b} \right)^2 = 1$

$x = a \sinh \theta$

Ans: B

JEE ADVANCED LEVEL

01 Short trick method

put $A = 0^\circ$

$\therefore \boxed{p = 1}, \boxed{q = 1}$

option: C: $p^3 - 3p + 2q = 1 - 3 + 2 = 0$

Ans: C

02 $\sec \theta + \tan \theta = x \rightarrow (1)$

$\sec \theta - \tan \theta = \frac{1}{x} \rightarrow (2)$

$(1) + (2) \Rightarrow 2 \sec \theta = x + \frac{1}{x}$

$\Rightarrow \sec \theta = \frac{1}{2} \left(x + \frac{1}{x} \right)$

$(1) - (2) \Rightarrow$

$\tan \theta = \frac{1}{2} \left(x - \frac{1}{x} \right)$

Ans: A, C

03 let $\theta = 45^\circ$

(5)

$$\left(\sqrt{2} - \frac{1}{\sqrt{2}}\right) \left(\sqrt{2} - \frac{1}{\sqrt{2}}\right) (1+1) = 1$$

Ans: B

04 Statement I: $\sin \theta + \cos \theta = x \Rightarrow \sin \theta \cos \theta = \frac{x^2 - 1}{2}$

$$\begin{aligned} (\sin^2 \theta)^3 + (\cos^2 \theta)^3 &= (\sin^2 \theta + \cos^2 \theta)^3 - 3 \sin^2 \theta \cos^2 \theta (\sin \theta + \cos \theta) \\ &= 1 - 3 \left(\frac{x^2 - 1}{2} \right)^2 (1) \\ &= \frac{4 - 3(x^2 - 1)^2}{4} \quad (\text{True}) \end{aligned}$$

Ans: A

Statement II: Conceptual (True)

05 Statement I: $x = a \sec \theta + b \tan \theta \rightarrow (1)$
 $y = a \tan \theta + b \sec \theta \rightarrow (2)$

$$(1)^2 - (2)^2 \Rightarrow x^2 - y^2 = a^2 - b^2 \quad (\text{True})$$

Statement II: $\sec \theta + \tan \theta = a$
 $\Rightarrow \sec \theta - \tan \theta = \frac{1}{a}$
 $\Rightarrow \tan \theta - \sec \theta = -\frac{1}{a} \quad (\text{True})$

Ans: A

06 Assertion: $\sec \theta + \tan \theta = x \rightarrow (1)$

$$\Rightarrow \sec \theta - \tan \theta = \frac{1}{x} \rightarrow (2)$$

$$\begin{aligned} (1) + (2) \Rightarrow 2 \sec \theta &= x + \frac{1}{x} = \frac{x^2 + 1}{x} \\ \Rightarrow \sec \theta &= \frac{x^2 + 1}{2x} \quad (\text{True}) \end{aligned}$$

Reason: Conceptual (True)

Ans: A



07. Assertion: Conceptual (False)

(6)

Reason: $\sec^2 \theta - \tan^2 \theta = 1 \quad \forall \theta \in \mathbb{R} - \left((2n+1)\frac{\pi}{2} \right)$
(~~False~~)
True

Ans: **B**

08 $\cos A + \cos^2 A = 1$
 $\Rightarrow \cos A = 1 - \cos^2 A$
 $\Rightarrow \cos A = \sin^2 A$
 $\Rightarrow \cos^2 A = \sin^4 A$

$$\begin{aligned} \sin^2 A + \sin^4 A \\ = \sin^2 A + \cos^2 A \\ = 1 \end{aligned}$$

Ans: B

Ans: B

09. put $\theta = 0$

10. put $\theta =$

~~let $\cos$~~

09. $\sin^4 A - 2\sin^2 A - \sin^8 A$
 $= \cos^2 A - 2\cos A - \cos^4 A$
 $= y^2 - 2y - y^4$
 $= y^2 - 2y - (1-y)^2$
 $= y^2 - 2y - 1 + 2y - y^2$
 $= -1$

let $y = \cos A$
 $\cos A + \cos^2 A = 1$
 $y + y^2 - 1 = 0$
 $\Rightarrow y^2 = 1 - y$
 $\Rightarrow y^4 = (1 - y)^2$

Ans: C

10.

10. Given $\cos x + \cos^3 x = 1$

(7)

$$\Rightarrow \cos^3 x = 1 - \cos x$$

$$\begin{aligned} \text{Now, } \cos^3 x &= \cos x \cdot \cos^2 x \\ &= \cos x (1 - \cos x) \\ &= \cos x - \cos^2 x \\ &= \cos x - (1 - \cos x) \\ &= 2\cos x - 1 \end{aligned}$$

$$\begin{aligned} \cos^6 x &= (\cos^3 x)^2 \\ &= (2\cos x - 1)^2 \\ &= 4\cos^2 x - 4\cos x + 1 \\ &= 4(1 - \cos x) - 4\cos x + 1 \\ &= 5 - 8\cos x \end{aligned}$$

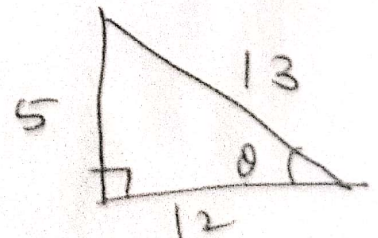
$$\begin{aligned} \text{Now, } \cos^6 x + 4\cos^3 x &= (5 - 8\cos x) + 4(2\cos x - 1) \\ &= 5 - 4 = 1 \end{aligned}$$

Ans: B

11. Given $\tan \theta = \frac{5}{12}$

$$\sin \theta = \frac{5}{13}$$

$$\Rightarrow \sin^2 \theta = \frac{25}{169}$$



Ans: A

12.

$$\sec \theta = \frac{13}{12} \Rightarrow \sec^2 \theta = \frac{169}{144}$$

(2)
Ans. B

13.

$$2 \sec \theta = x + \frac{1}{x} ; 2 \tan \theta = x - \frac{1}{x}$$

$$4(\sec^2 \theta - \tan^2 \theta) = \left(x + \frac{1}{x}\right)^2 - \left(x - \frac{1}{x}\right)^2$$

$$\left(x + \frac{1}{x}\right)^2 - \left(x - \frac{1}{x}\right)^2 = \frac{1}{4} = 0.25$$

Integral value = 0

Ans. 0

14.

NOTE: Please, discard this question as it has insufficient data

15.

a) let $\theta = 45^\circ$

$$\begin{array}{l|l} 1+1=m & \sqrt{2} - \frac{1}{\sqrt{2}} = n \\ \Rightarrow \boxed{m=2} & \Rightarrow \boxed{n = \frac{1}{\sqrt{2}}} \end{array}$$

Now, $(m^2 n)^{2/3} - (m n^2)^{2/3}$

$$= \left(4 \cdot \frac{1}{\sqrt{2}}\right)^{2/3} - \left(2 \cdot \frac{1}{2}\right)^{2/3}$$

$$= (2\sqrt{2})^{2/3} - 1^{2/3}$$

$$= \left(2^{3/2}\right)^{2/3} - 1 = 2 - 1 = 1 \text{ (a)}$$

b) let $\theta = 45^\circ$

$$m = \sqrt{2} - \frac{1}{\sqrt{2}} \quad | \quad n = \sqrt{2} - \frac{1}{\sqrt{2}}$$

$$m = \frac{1}{\sqrt{2}} \quad | \quad n = \frac{1}{\sqrt{2}}$$

$$(mn)^{\frac{2}{3}} - (m n^2)^{\frac{2}{3}}$$

$$= \left(\frac{1}{2} \cdot \frac{1}{\sqrt{2}}\right)^{\frac{2}{3}} - \left(\frac{1}{\sqrt{2}} \cdot \frac{1}{2}\right)^{\frac{2}{3}} = 0 \quad \underline{(q)}$$

c) let $\alpha = 0^\circ$

$$x = a \Rightarrow (x - a) = 0$$

$$\text{Now } (x - a)(y - a) + (x - y)^2 \sin^2 \alpha \cdot \cos^2 \alpha$$

$$= (0)(y - a) + (x - y)^2 \sin^2 0^\circ \cdot \cos^2 0^\circ$$

$$= 0 \quad (q)$$

d) let $\alpha = \beta = \gamma = 0^\circ$

$$\Rightarrow x = r, y = 0, z = 0, \gamma = 0$$

$$\text{Now, } x^2 + y^2 + z^2 + \gamma^2 = r^2 (s)$$

Ans: $r, \underline{q}, q, s$

$$\boxed{16} \quad a) (\tan \theta + \cot \theta)^2 = \tan^2 \theta + \cot^2 \theta + 2 \tan \theta \cot \theta$$

$$= \tan^2 \theta + \cot^2 \theta + 2 \quad (P)$$

$$\boxed{b) \tan^2 \theta + \cot^2 \theta = (\tan \theta + \cot \theta)^2 - 2 \tan \theta \cot \theta}$$

$$= \underline{(\tan \theta + \cot \theta)^2 - 2} \quad (—)$$

c) Conceptual (r)

d) Conceptual (s)

Ans: P, —, r, s

LEARNERS TASK (CUE'S) (10)

01. ~~$xy = m \sec \theta \cdot n \tan \theta$~~

$$\frac{x}{m} = \sec \theta, \quad \frac{y}{n} = \tan \theta$$

$$\Rightarrow \frac{x^2}{m^2} - \frac{y^2}{n^2} = 1$$

Ans: B

Ans: B

02. $xy = 1$

03. $\frac{a}{x} = \csc \theta$; $\frac{b}{y} = \cot \theta$

$$\Rightarrow \left(\frac{a}{x}\right)^2 - \left(\frac{b}{y}\right)^2 = 1$$

Ans: B

04. $xy = ab \Rightarrow x^2 y^2 = a^2 b^2$

Ans: D

05. $xy = ab$

Ans: C

06

Short cut method

(11)

$$\text{let } \theta = 45^\circ$$

$$x = 1 + \frac{1}{\sqrt{2}}$$

$$y = 1 - \frac{1}{\sqrt{2}}$$

$$x + y = 2$$

$$x - y = \frac{2}{\sqrt{2}} = \sqrt{2}$$

$$\text{Now } (x^2 - y^2)^2 = [(x+y)(x-y)]^2 \\ = [2 \cdot \sqrt{2}]^2 = 8$$

$$\text{option B: } 16xy = 16\left(1 + \frac{1}{\sqrt{2}}\right)\left(1 - \frac{1}{\sqrt{2}}\right) \\ = 16\left(1 - \frac{1}{2}\right) = 16 \times \frac{1}{2} = 8$$

Ans. B

07.

$$\frac{x}{a} = \sin \theta$$

$$\Rightarrow \frac{a}{x} = \csc \theta$$

$$y = b \tan \theta$$

$$\Rightarrow \frac{b}{y} = \cot \theta$$

$$\Rightarrow \frac{a^2}{x^2} - \frac{b^2}{y^2} = 1$$

Ans: A

08

$$x^2 - y^2 = 4$$

Ans. D

09

$$2(\sin^2 \theta + \cos^2 \theta) = 2(1) = 2$$

Ans. A

10

$$x = at, \quad y = \frac{a}{t}$$

$$\Rightarrow xy = a^2$$

Ans. B



$$\frac{x}{a} = \tan \theta, \quad \frac{y}{b} = \sec \theta$$

$$\Rightarrow \left(\frac{y}{b}\right)^2 - \left(\frac{x}{a}\right)^2 = 1 \quad \text{or} \quad \left(\frac{x}{a}\right)^2 - \left(\frac{y}{b}\right)^2 = -1$$

Ans: A

$$xy = pq(\cot^2 \theta - \sec^2 \theta)$$

$$\Rightarrow xy = -pq$$

$$\Rightarrow \frac{x}{p} = -\frac{q}{y}$$

Ans: B

$$p^2 + q^2 = (\cos \theta + \sin \theta)^2 + (\sin \theta - \cos \theta)^2$$

$$= 2$$

$$\Rightarrow p^2 - 2 = -q^2$$

Ans: B

$$p \cos \theta + q \sin \theta = x \rightarrow (1)$$

$$p \sin \theta - q \cos \theta = y \rightarrow (2)$$

$$(1)^2 + (2)^2 \Rightarrow p^2 + q^2 = x^2 + y^2$$

$$\Rightarrow x^2 - p^2 = q^2 - y^2$$

Ans: C

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

Ans: B

$$\cancel{x^2 + y^2 + z^2 = r^2}$$

Ans:

$$\text{Let } \theta = \phi = 0^\circ$$

$$\therefore x = r; \quad y = 0, \quad z = 0$$

$$\therefore x^2 + y^2 + z^2 = r^2$$

Ans: C

07. $\frac{x}{a} = \sin^4 \theta ; \frac{y}{b} = \cos^4 \theta$

(13)

$$\Rightarrow \sqrt{\frac{x}{a}} + \sqrt{\frac{y}{b}} = 1$$

Ans: C

08. Let $\theta = 0^\circ$ $\left| \begin{array}{l} a^2 - b^2 = x^2 - y^2 \\ x = a \\ y = b \end{array} \right.$

Ans: B

09. Let $\phi = \theta = 0^\circ$
 $\left. \begin{array}{l} a = 1 \\ b = 0 \\ c = 0 \end{array} \right\} \quad a^2 + b^2 + c^2 = 1$

Ans: D

10. Let $\theta = 45^\circ$
 $x = a \left(\frac{1}{\sqrt{2}} \right)^2 \cdot \left(\frac{1}{\sqrt{2}} \right)$
 $x = \frac{a}{2\sqrt{2}}$
 $y = \frac{a}{2\sqrt{2}}$

$$x^2 + y^2 = \frac{a^2}{8} + \frac{a^2}{8} = \frac{a^2}{4}$$

$$x^2 y^2 = \frac{a^4}{64}$$

$$\frac{(x^2 + y^2)^3}{x^2 y^2} = \frac{a^6}{64} \times \frac{64}{a^4} = a^2$$

Ans: C

JEE ADVANCED

01. $x^2 - y^2 = a$

$$\Rightarrow (x+y)(x-y) - a = 0$$

$$\Rightarrow \cancel{x^2 - y^2 = a}$$

$\Rightarrow$

Ans: B, C



02 Let $\theta = 45^\circ$

(14)

$$= (1+1+\sqrt{2})(1+1-\sqrt{2})$$

$$= (2+\sqrt{2})(2-\sqrt{2}) = 4-2 = 2$$

Ans: C

03 Statement I: Let $\theta = \phi = 0$

$$l = p, m = 0, n = 0.$$

$$\therefore \frac{l^2}{p^2} + \frac{m^2}{q^2} + \frac{n^2}{r^2} = 1 \quad (\text{True})$$

Statement II: $\frac{\sin \theta}{1 - \cos \theta} = \frac{1 + \cos \theta}{\sin \theta}$

$$\Rightarrow \sin^2 \theta = 1 - \cos^2 \theta \quad (\text{True})$$

$$(\tan \theta + \sec \theta)(\tan \theta - \sec \theta) = 1$$

$$\Rightarrow \tan^2 \theta - \sec^2 \theta = 1$$

$$\Rightarrow -1 = 1 \quad (\text{False})$$

Ans: B

04 Statement I:

$$\text{Let } \theta = 45^\circ$$

$$l = \sqrt{2} - \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

$$m = \sqrt{2} - \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$$

Statement II:

$$\frac{\cos \theta}{1 - \sin \theta} = \frac{1 + \sin \theta}{\cos \theta}$$

$$\Rightarrow \cos^2 \theta = 1 - \sin^2 \theta \quad (\text{True})$$

$$\text{Now, } l^2 + m^2 + 3 =$$

$$= \frac{1}{2} \cdot \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + 3 \right)$$

$$= \frac{1}{4} (4)$$

$$= 1 \quad (\text{True})$$

$$\frac{\sin \theta}{1 + \sin \theta} = \frac{\cos \theta}{1 + \cos \theta}$$

(False)

Ans: B C

Q5 Assertion: $\sin \theta \cdot \cos \theta = \frac{1}{2}$

(15)

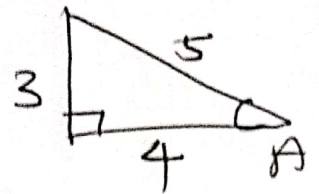
Let $\theta = 45^\circ$ satisfies the above eqn.

$\therefore \sin 2\theta = \sin 2 \times 45^\circ = \sin 90^\circ = 1$ (True)

Reason: Conceptual (True)

Ans: A

Q6 Assertion: $\sin A = \frac{3}{5}$
 $\therefore \tan A = \frac{3}{4}$ (True)



Reason: $\sin A = \frac{3}{5}$

$\Rightarrow \cos A = \frac{4}{5}$ and $\tan A = \frac{3}{4}$ (True)

Ans: A

Q7 $\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1 \rightarrow (1)$
 $\frac{x}{a} \sin \theta - \frac{y}{b} \cos \theta = 1 \rightarrow (2)$

$(1)^2 + (2)^2 \Rightarrow \frac{x^2}{a^2} + \frac{y^2}{b^2} = 2$

$\Rightarrow a^2 y^2 + b^2 x^2 = 2a^2 b^2$

Ans: D

Q8 $a^2 y^2 + b^2 x^2 = 2a^2 b^2$

$a = 2, b = 2$

$4y^2 + 4x^2 = 2 \cdot 4 \cdot 4$

$\Rightarrow x^2 + y^2 = 8$

Ans: C

Q9 $\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1$

$\theta = 45^\circ, a = 2, b = 2$

$\frac{x}{2} \cdot \frac{1}{\sqrt{2}} + \frac{y}{2} \cdot \frac{1}{\sqrt{2}} = 1$

$x + y = 2\sqrt{2}$

Ans: A

$$10. \cos \theta = \frac{4}{5} \Rightarrow \sec \theta = \frac{5}{4}$$

(16)
Ans: B

11

$$\tan^2 \theta + 1 = \left(\frac{3}{4}\right)^2 + 1 = \frac{25}{16}$$

Ans: A

12

$$\frac{U}{l} = \tan \theta, \quad \frac{V}{m} = \sin \theta$$

$$\Rightarrow \frac{l}{U} = \cot \theta, \quad \frac{m}{V} = \operatorname{cosec} \theta$$

$$\Rightarrow \frac{m^2}{V^2} - \frac{l^2}{U^2} = 1$$

Ans: 1

13

$$\text{put } \theta = \phi = 0^\circ$$

$$\therefore x = r, \quad y = 0, \quad z = 0$$

$$\therefore x^2 + y^2 + z^2 = r^2$$

NOTE: Please discard this problem, as it has insufficient data

14

$$a) y^2 = 4ax$$

$$(2at)^2 = 4a(at^2)$$

$$\Rightarrow 4a^2t^2 = 4a^2t^2(x)$$

$$b) xy = (at)\left(\frac{a}{t}\right) = a^2(y)$$

$$c) \frac{x}{a} = \sec \theta, \quad \frac{y}{a} = \tan \theta$$

$$\left(\frac{x}{a}\right)^2 - \left(\frac{y}{a}\right)^2 = 1 \Rightarrow x^2 - y^2 = a^2(p)$$

$$d) \left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1 (s)$$

Ans: x, y, p, s

15 a) option verification

$$(t) \quad \frac{x-h}{r} = \sin \theta, \quad \frac{y-k}{r} = \cos \theta$$

$$\Rightarrow \left(\frac{x-h}{r}\right)^2 + \left(\frac{y-k}{r}\right)^2 = 1$$

$$b)(\delta) \quad \frac{x+h}{r} = \cos \theta, \quad \frac{y+k}{r} = \sin \theta$$

$$\Rightarrow \left(\frac{x+h}{r}\right)^2 + \left(\frac{y+k}{r}\right)^2 = 1$$

$$c)(\alpha) \quad \frac{x-k}{r} = \cos \theta, \quad \frac{y-h}{r} = \sin \theta$$

$$\left(\frac{x-k}{r}\right)^2 + \left(\frac{y-h}{r}\right)^2 = 1$$

$$d)(\rho) \quad \frac{x+k}{r} = \sin \theta, \quad \frac{y+h}{r} = \cos \theta$$

$$\left(\frac{x+k}{r}\right)^2 + \left(\frac{y+h}{r}\right)^2 = 1$$

Ans: t, r, \alpha, \rho

ADDITIONAL PRACTICE QUESTIONS

01. $xy = a^2 b^2 (\sec \theta - \tan \theta)^2$

$$\Rightarrow xy = a^2 b^2$$

Ans: A

02. $x = 1(2 + \sqrt{3})^2 = 7 + 4\sqrt{3} \Rightarrow x^2 = 97 + 56\sqrt{3}$

$$y = 1(2 - \sqrt{3})^2 = 7 - 4\sqrt{3} \Rightarrow y^2 = 97 - 56\sqrt{3}$$

$$\therefore x^2 + y^2 = 194$$

Ans: C

03

$$x = \frac{1}{4} (\sqrt{2} + 1)^2 = \frac{1}{4} (3 + 2\sqrt{2})$$

(18)

$$y = \frac{1}{4} (\sqrt{2} - 1)^2 = \frac{1}{4} (3 - 2\sqrt{2})$$

$$x^2 - y^2 = \frac{1}{16} [(3 + 2\sqrt{2})^2 - (3 - 2\sqrt{2})^2]$$

$$= \frac{1}{16} [4 \cdot 3 \cdot 2\sqrt{2}] = \frac{3\sqrt{2}}{2}$$

Ans: C

$\Rightarrow$ THE END $\Leftarrow$

