

CHAPTER : Angles in Quadrants (signs) Teaching Task

1. Given $\sin \alpha + \operatorname{cosec} \alpha = 2$

$$\Rightarrow \sin \alpha + \frac{1}{\sin \alpha} = 2$$

$$\Rightarrow \sin^2 \alpha + 1 = 2 \sin \alpha$$

$$\Rightarrow \sin^2 \alpha - 2 \sin \alpha + 1 = 0$$

$$\Rightarrow (\sin \alpha - 1) = 0$$

$$\Rightarrow \sin \alpha = 1$$

$$\Rightarrow \alpha = \frac{\pi}{2}$$

$$\text{Now } \sin^n \alpha + \operatorname{cosec}^n \alpha = \sin^n \frac{\pi}{2} + \operatorname{cosec}^n \frac{\pi}{2} = (1)^n + (1)^n = 2$$

Ans : C

2. $\tan(855^\circ) = \tan(2^2 \times 360^\circ + 135^\circ)$
 $= \tan 135^\circ$
 $= \tan(180^\circ - 45^\circ)$
 $= -\tan 45^\circ$
 $= -1$

Ans : B

3. given $\alpha = n\pi - \theta$

$$\text{Now } \sin \alpha = \sin(n\pi - \theta)$$

$$= (-1)^{n+1} \sin \theta$$

Ans : A

4. $\cos \left[(2n+1) \frac{\pi}{2} - \theta \right] = (-1)^n \cdot \sin \theta$

Ans : B

5. $\alpha = \theta - \frac{13\pi}{2}$

$$\cot \alpha = \cot \left(\theta - \frac{13\pi}{2} \right)$$

$$= -\cot \left(\frac{13\pi}{2} - \theta \right)$$

$$= -\tan \theta$$

$$= \text{since } \cot\left((2n+1)\frac{\pi}{2} - \theta\right) = \tan\theta$$

Ans : C

6. Given $\sin\theta = \frac{4}{5}$, which is positive value

$$\Rightarrow \theta \in Q_1 \text{ or } Q_2$$

But given $\theta \notin Q_1$, therefore $\theta \in Q_2$

$$\therefore \cos\theta = -\frac{3}{5}$$

Ans : C

7. Given θ is any angle

complement of θ is $\frac{\pi}{2} - \theta$

supplement of θ is $\pi - \theta$

$$\therefore \text{sum} = \frac{\pi}{2} - \theta + \pi - \theta$$

$$= \frac{3\pi}{2} - 2\theta$$

Ans : D

8. $\sin\left(\frac{-11\pi}{3}\right) = -\sin\left(\frac{11\pi}{3}\right) = -\sin\left(4\pi - \frac{\pi}{3}\right)$

$$\sin\frac{\pi}{3} = \frac{\sqrt{3}}{2}$$

$$\tan\left(\frac{35\pi}{6}\right) = \tan\left(6\pi - \frac{\pi}{6}\right) = -\tan\frac{\pi}{6} = -\frac{1}{\sqrt{3}}$$

$$\sec\left(-\frac{7\pi}{6}\right) = \sec\left(\frac{7\pi}{6}\right) = \sec\left(\pi + \frac{\pi}{6}\right) = -\sec\frac{\pi}{6} = -\frac{2}{\sqrt{3}}$$

$$\cos\left(\frac{5\pi}{4}\right) = \cos\left(\pi + \frac{\pi}{4}\right) = -\cos\frac{\pi}{4} = -\frac{1}{\sqrt{2}}$$

$$\operatorname{cosec}\left(\frac{7\pi}{4}\right) = \operatorname{cosec}\left(2\pi - \frac{\pi}{4}\right) = -\operatorname{cosec}\frac{\pi}{4} = -\sqrt{2}$$

$$\cos\left(\frac{17\pi}{6}\right) = \cos\left(2\pi + \frac{5\pi}{6}\right) = \cos\frac{5\pi}{6} = \cos\left(\pi - \frac{\pi}{6}\right)$$

$$= -\cos \frac{\pi}{6} = -\frac{\sqrt{3}}{2}$$

$$\text{Given problem} = \frac{\left(\frac{\sqrt{3}}{2}\right)\left(\frac{-1}{\sqrt{3}}\right)\left(-\frac{2}{\sqrt{3}}\right)}{\left(\frac{-1}{\sqrt{2}}\right)(\sqrt{2})\left(\frac{-\sqrt{3}}{2}\right)}$$

$$= -\frac{\left(\frac{1}{\sqrt{3}}\right)}{\left(\frac{\sqrt{3}}{2}\right)} = -\frac{2}{3}$$

$$\text{Ans : } -\frac{2}{3}$$

9. Given $a \cos \theta - b \sin \theta = c$ (1)

let $a \sin \theta + b \cos \theta = x$ (2)

$$(1)^2 + (2)^2 \Rightarrow a^2(\cos^2 \theta + \sin^2 \theta) + b^2(\sin^2 \theta + \cos^2 \theta) = c^2 + x^2$$

$$\Rightarrow a^2 + b^2 = c^2 + x^2$$

$$\Rightarrow x^2 = a^2 + b^2 - c^2$$

$$\Rightarrow x = \pm \sqrt{a^2 + b^2 - c^2}$$



Educational Operating System

ANS : D

10. Given $8 \tan A = -15$

$$\Rightarrow \tan A = -\frac{15}{8}$$

$$25 \sin B = -7$$

$$\Rightarrow \sin B = \frac{-7}{25}$$

given neither A nor B is in the 4th Quadrant

therefore $A \in Q_2$ and $B \in Q_3$

$$\text{we have } \sin A = \frac{15}{17}, \cos A = -\frac{8}{17}, \cos B = -\frac{24}{25}$$

Now, $\sin A \cos B + \cos A \sin B$

$$= \frac{15}{17} \cdot \frac{-24}{25} + \frac{-8}{17} \cdot \frac{-7}{25}$$

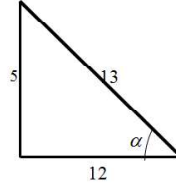
$$= -\frac{360}{425} + \frac{56}{425} = -\frac{304}{425}$$

Ans : C

11. given $\sin \alpha = \frac{5}{13}$ and $\frac{\pi}{2} < \alpha < \pi$
i.e α lies in the second quadrant

$$\text{Now } = \frac{\sec \alpha + \tan \alpha}{\operatorname{cosec} \alpha - \cot \alpha}$$

$$= \frac{\left(\frac{-13}{12}\right) + \left(\frac{-5}{12}\right)}{\frac{13}{5} - \left(-\frac{12}{5}\right)} = -0.3$$



Ans : C

12. Given $\frac{D}{90} = \frac{G}{100} = \frac{2C}{\pi}$

$$\Rightarrow D = \frac{180C}{\pi}, G = \frac{200C}{\pi}$$

$$\text{Now } G - D = \frac{200C}{\pi} - \frac{180C}{\pi} = \frac{20C}{\pi}$$

Ans : A

13. We have $\sin(90^\circ + \theta) = \cos \theta$
 $\sin(90^\circ - \theta) = \cos \theta$

Ans : A,D

14. given $\sin^2 \theta + \cos^2 \theta = 1$

$$\begin{aligned} \text{Option A : } \frac{\sin \theta}{1 - \cos \theta} \times \frac{1 + \cos \theta}{1 + \cos \theta} &= \frac{\sin \theta (1 + \cos \theta)}{1 - \cos^2 \theta} \\ &= \frac{\sin \theta (1 + \cos \theta)}{\sin^2 \theta} \\ &= \frac{1 + \cos \theta}{\sin \theta} \end{aligned}$$

$$\begin{aligned} \text{Option B : } \frac{\cos \theta}{1 + \sin \theta} \times \frac{1 - \sin \theta}{1 - \sin \theta} &= \frac{\cos \theta (1 - \sin \theta)}{1 - \sin^2 \theta} \\ &= \frac{\cos \theta (1 - \sin \theta)}{\cos^2 \theta} \end{aligned}$$

$$= \frac{1 - \sin \theta}{\cos \theta}$$

Ans : A, B

15. Statement - I : $l = r\theta$, is correct

Statement - II : given $l = 15\text{cm}$, $\theta = 30^\circ$

$$\text{Now } r = \frac{l}{\theta}$$

$$\Rightarrow r = \frac{15}{\left(\frac{\pi}{6}\right)} = \frac{15 \times 6}{\pi} = \frac{15 \times 6 \times 7}{22}$$

$$= \frac{315}{11} = 28\frac{7}{11}$$

Ans : A

16. Statement - I $\frac{D}{90} = \frac{G}{100} = \frac{2C}{\pi}$, which is true

Statement - II given $D = 45^\circ$
 $G = 50$

$$\therefore \frac{45}{90} = \frac{2C}{\pi}$$

$$\Rightarrow C = \frac{\pi}{4} = \frac{11}{4}$$

Ans : C

17. Statement I : Given $A + B = 90^\circ$

$$\Rightarrow \cot(A + B) = \cot 90^\circ$$

$$\Rightarrow \frac{\cot A \cot B - 1}{\cot A + \cot B} = 0$$

$$\Rightarrow \cot A \cdot \cot B = 1$$

$$\text{statement II : } \cot \frac{\pi}{20} \cdot \cot \frac{5\pi}{20} \cdot \cot \frac{7\pi}{20} \cdot \cot \frac{9\pi}{20}$$

$$= \cot \frac{\pi}{20} \cdot \cot \frac{5\pi}{20} \cdot \cot \left(\frac{\pi}{2} - \frac{3\pi}{20} \right) \cdot \cot \left(\frac{\pi}{2} - \frac{\pi}{20} \right)$$

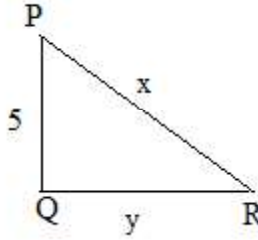
$$= \cot \frac{\pi}{20} \cdot \cot \frac{5\pi}{20} \cdot \tan \frac{3\pi}{20} \cdot \tan \frac{\pi}{20}$$

$$= \left(\cot \frac{\pi}{20} \cdot \tan \frac{\pi}{20} \right) \cdot \cot \frac{\pi}{4} \cdot \tan \frac{3\pi}{20}$$

$$= 1 \times 1 \times \tan \frac{3\pi}{20} = \tan \frac{3\pi}{20}$$

Ans : B

18. given $x+y=25$
 we have $5^2+x^2=y^2$
 $\Rightarrow 25+x^2=(25-x)^2$
 $\Rightarrow 25+x^2=625-50x+x^2$
 $\Rightarrow 50x=600$
 $\Rightarrow x=12, y=13$
 $\therefore PQ=5, QR=12, PR=13$
 $QR=12\text{cm}$



Ans : B

19. $\sin P = \frac{QR}{PR} = \frac{12}{13}$

Ans ; B

20. $\cos R = \frac{QR}{PR} = \frac{12}{13}$

Ans : D

21. We have $A+B+C = \pi$

$$\Rightarrow A+B = \pi - C$$

$$\Rightarrow \tan(A+B) = \tan(\pi - C)$$

$$\frac{\tan A + \tan B}{1 - \tan A \tan B} = -\tan C$$

$$\Rightarrow \tan A + \tan B = -\tan C + \tan A \tan B \tan C$$

$$\Rightarrow \tan A + \tan B + \tan C = \tan A \tan B \tan C$$

$$\Rightarrow \tan A + \tan B + \tan C - \tan A \tan B \tan C = 0$$

22. a) $\frac{\tan(180^\circ + A) \cdot \tan(270^\circ + A) \cdot \sin(360^\circ - A)}{\cos(180^\circ - A) \cdot \cot(90^\circ + A) \cdot \cos(-A)}$

$$= \frac{\tan A - \cot A - \sin A}{-\cos A - \tan A \cos A}$$

$$= \frac{1}{\cos A}$$

b) $\frac{\sin(-A) \cdot \cos(180^\circ - A)}{\sin A}$

$$= \frac{-\sin A - \cos A}{\sin A} = \cos A$$

$$\begin{aligned} \text{c) } & \sin^2(180^\circ - A) + \cos^2(180^\circ - A) \\ &= \sin^2 A + \cos^2 A \\ &= 1 \end{aligned}$$

$$\text{d) } \frac{\sin\left(\frac{-11\pi}{3}\right) \cdot \sec\left(\frac{-7\pi}{3}\right)}{\cot\left(\frac{5\pi}{4}\right) \cdot \operatorname{cosec}\left(\frac{7\pi}{4}\right)}$$

$$= \frac{-\sin\left(\frac{11\pi}{3}\right) \cdot \sec\left(\frac{7\pi}{3}\right)}{\cot\left(\frac{5\pi}{4}\right) \cdot \operatorname{cosec}\left(\frac{7\pi}{4}\right)}$$

$$= \frac{-\sin\left(4\pi - \frac{\pi}{3}\right) \cdot \sec\left(2\pi + \frac{\pi}{3}\right)}{\cot\left(\pi + \frac{\pi}{4}\right) \cdot \operatorname{cosec}\left(2\pi - \frac{\pi}{4}\right)}$$

$$= \frac{\sin \frac{\pi}{3} \cdot \sec \frac{\pi}{3}}{\cot \frac{\pi}{4} \cdot -\operatorname{cosec} \frac{\pi}{4}}$$

$$= \frac{\left(\frac{\sqrt{3}}{2}\right) \cdot 2}{1 \cdot -\sqrt{2}} = -\sqrt{\frac{3}{2}}$$

EdoS
Educational Operating System

Ans : a-s, b-t, c-q, d-r

Learners Task

$$\begin{aligned} 1. \quad & 135 = 135 \times 1^0 \\ &= 135 \times \frac{\pi}{180} = \frac{3\pi}{4} \text{ radians} \end{aligned}$$

Ans : C

$$2. \quad 1 \text{ grades} = 100 \text{ minutes}$$

Ans : B

3. Given $\cos 7A = \sin(A-6)$
 $\Rightarrow 7A + A - 6^\circ = 90^\circ$
 $\Rightarrow 8A = 96^\circ$
 $\Rightarrow A = 12^\circ$

Ans : A

4. $\cot(360^\circ - \theta) = -\cot \theta$

Ans : B

5. we have $\sec^2 \theta - \tan^2 \theta = 1$
 $\Rightarrow (\sec \theta + \tan \theta)(\sec \theta - \tan \theta) = 1$
 $\Rightarrow \sec \theta + \tan \theta = \frac{1}{\sec \theta - \tan \theta}$

Ans : B

6. $\cot^2 \theta - \operatorname{cosec}^2 \theta = -(\operatorname{cosec}^2 \theta - \cot^2 \theta)$
 $= -1$

Ans : D

7. Given $\operatorname{cosec} \theta + \cot \theta = k$

$$\Rightarrow \operatorname{cosec} \theta - \cot \theta = \frac{1}{k}$$

$$\Rightarrow \cot \theta - \operatorname{cosec} \theta = \frac{-1}{k}$$

Ans : B

8. We know $\operatorname{cosec}^2 \theta - \cot^2 \theta = 1$

$$\Rightarrow \operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$$

$$\Rightarrow \operatorname{cosec} \theta = \pm \sqrt{1 + \cot^2 \theta}$$

Ans : C

9. $\sin \theta \cdot \cot \theta + \cos \theta \cdot \tan \theta$

$$= \sin \theta \cdot \frac{\cos \theta}{\sin \theta} + \cos \theta \cdot \frac{\sin \theta}{\cos \theta}$$

$$= \cos \theta + \sin \theta$$

Ans : A

$$\begin{aligned}
 10. \quad & \sin 30^\circ \cdot \cos 60^\circ + \cos 30^\circ \cdot \sin 60^\circ \\
 &= \sin(30^\circ + 60^\circ) \\
 &= \sin 90^\circ \\
 &= 1
 \end{aligned}$$

Ans :B

JEE MAINS

$$\begin{aligned}
 1. \quad & \text{Given } \cot \theta = \frac{7}{8} \\
 & \frac{(1 + \sec \theta)(1 - \sin \theta)}{(1 + \cos \theta)(1 - \cos \theta)} = \frac{1 - \sin^2 \theta}{1 - \cos^2 \theta} = \frac{\cos^2 \theta}{\sin^2 \theta} \\
 &= \cot^2 \theta \\
 &= \left(\frac{7}{8}\right)^2 \\
 &= \frac{49}{64}
 \end{aligned}$$

Ans : A

$$\begin{aligned}
 2. \quad & \text{Given } \operatorname{cosec} A = \sqrt{10} \\
 & \text{we have } \cot^2 A = \operatorname{cosec}^2 A - 1 \\
 &= 10 - 1 \\
 &= 9
 \end{aligned}$$

$$\therefore \cot A = 3$$

And : D

$$\begin{aligned}
 3. \quad & \text{given } \sec \theta - \tan \theta = 3 \quad \dots\dots\dots(1) \\
 & \Rightarrow \sec \theta - \tan \theta = \frac{1}{3} \quad \dots\dots\dots(2)
 \end{aligned}$$

$$(1) + (2) \Rightarrow 2 \sec \theta = \frac{10}{3} \Rightarrow \sec \theta = \frac{5}{3}$$

$$(1) - (2) \Rightarrow -2 \tan \theta = \frac{8}{3} \Rightarrow \tan \theta = -\frac{4}{3}$$

$\sec \theta$ is +ve and $\tan \theta$ is -ve

$\therefore \theta$ belongs to 4th quadrant

And : D

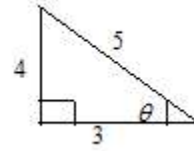
$$4. \quad \text{Given '}\theta\text{' is not in the 4th quadrant}$$

$$\therefore \tan \theta = \frac{-4}{3} \quad \therefore \theta \in Q_2$$

$$\text{Now, } 5 \sin \theta + 10 \cos \theta + 9 \sec \theta$$

$$\begin{aligned}
 &= 5\left(\frac{4}{5}\right) + 10\left(\frac{-3}{5}\right) + 9\left(\frac{-5}{3}\right) \\
 &= 4 - 6 - 15 \\
 &= -17
 \end{aligned}$$

Ans : C



$$\begin{aligned}
 5. \quad & \sec\left(\frac{13\pi}{3}\right) \\
 &= \sec\left(4\pi + \frac{\pi}{3}\right) \\
 &= \sec\frac{\pi}{3} \\
 &= 2
 \end{aligned}$$

Ans : A

$$6. \quad \cot\frac{\pi}{16} \cdot \cot\frac{2\pi}{16} \cdot \cot\frac{3\pi}{16} \cdot \cot\frac{4\pi}{16} \cdot \cot\frac{5\pi}{16} \cdot \cot\frac{6\pi}{16} \cdot \cot\frac{7\pi}{16}$$

$$\text{Now, } \cot\frac{5\pi}{16} = \cot\left(\frac{\pi}{2} - \frac{3\pi}{16}\right) = \tan\frac{3\pi}{16}$$

$$= \cot\frac{6\pi}{16} = \cot\left(\frac{\pi}{2} - \frac{2\pi}{16}\right) = \tan\frac{2\pi}{16}$$

$$= \cot\frac{7\pi}{16} = \cot\left(\frac{\pi}{2} - \frac{\pi}{16}\right) = \tan\frac{\pi}{16}$$

$$\text{clearly } \cot\frac{4\pi}{16} = \cot\frac{\pi}{4} = 1$$

$$\therefore \cot\frac{\pi}{16} \cdot \cot\frac{2\pi}{16} \cdot \cot\frac{3\pi}{16} \cdot 1 \cdot \tan\frac{2\pi}{16} \cdot \tan\frac{\pi}{16}$$

$$= \left(\cot\frac{\pi}{16} \cdot \tan\frac{\pi}{16}\right) \left(\cot\frac{2\pi}{16} \cdot \tan\frac{2\pi}{16}\right) \left(\cot\frac{3\pi}{16} \cdot \tan\frac{3\pi}{16}\right)$$

$$= 1 \times 1 \times 1 = 1$$

$$7. \quad \frac{\cos(\pi - A) \cdot \cot\left(\frac{\pi}{2} + A\right) \cdot \cos(-A)}{\tan(\pi + A) \cdot \tan\left(\frac{3\pi}{2} + A\right) \cdot \sin(2\pi - A)}$$

$$= \frac{-\cos A - \tan A \cdot \cos A}{\tan A - \cot A - \sin A} = \cos A$$

Ans : C

8. given $\cos A = \cos B = -\frac{1}{2}$

$$\cos A = -\frac{1}{2}$$

$$\Rightarrow A \in Q_2 \text{ or } Q_3$$

given $A \notin Q_2$

$$\therefore A \in Q_3$$

now $\cos B = -\frac{1}{2}$

$$\Rightarrow B \in Q_2 \text{ or } Q_3$$

given $B \notin Q_3$

$$\therefore B \in Q_2$$

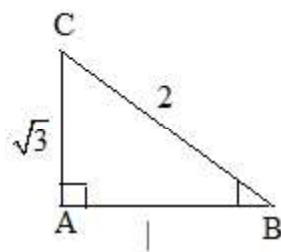
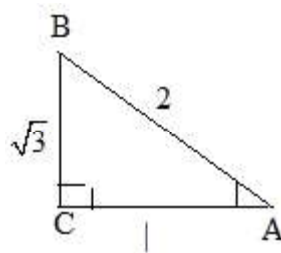
Now $\cos A = -\frac{1}{2}$

$$\sin A = \frac{-\sqrt{3}}{2}$$

also $\cos B = \frac{-1}{2}$

$$\sin B = \frac{\sqrt{3}}{2}$$

$$\tan B = -\sqrt{3}$$



$$\text{now } \frac{4\sin B - 3\tan A}{\tan B + \sin A} = \frac{4\left(\frac{\sqrt{3}}{2}\right) - 3(\sqrt{3})}{(-\sqrt{3}) + \left(\frac{-\sqrt{3}}{2}\right)}$$

$$= \frac{-\sqrt{3}}{\left(\frac{3\sqrt{3}}{2}\right)} = \frac{2}{3}$$

Ans : B

9. given $3\sin \theta + 4\cos \theta = 5$ (1)

Let $4\sin \theta - 3\cos \theta = x$ (2)

$$(1)^2 + (2)^2 \Rightarrow 9(\sin^2 \theta + \cos^2 \theta) + 16(\sin^2 \theta + \cos^2 \theta) = 25 + x^2$$

$$\Rightarrow 9 + 16 = 25 + x^2$$

$$\Rightarrow x=0$$

Ans : C

10. given $\frac{\cos A}{\cos B} = n$ and $\frac{\sin A}{\sin B} = m$

$$\Rightarrow \cos A = n \cos B \quad \text{and} \quad \sin A = m \sin B$$

$$\Rightarrow \cos^2 A = n^2 \cos^2 B \quad \text{and} \quad \sin^2 A = m^2 \sin^2 B$$

$$\Rightarrow \cos^2 A + \sin^2 A = n^2 \cos^2 B + m^2 \sin^2 B$$

$$\Rightarrow 1 = n^2 (1 - \sin^2 B) + m^2 \sin^2 B$$

$$\Rightarrow 1 = n^2 - n^2 \sin^2 B + m^2 \sin^2 B$$

$$\Rightarrow 1 = n^2 + (m^2 - n^2) \sin^2 B$$

$$\Rightarrow (m^2 - n^2) \sin^2 B = 1 - n^2$$

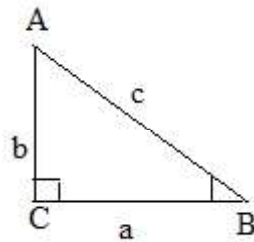
Ans : A

11. $\tan A + \tan B$

$$= \frac{a}{b} + \frac{b}{a}$$

$$= \frac{a^2 + b^2}{ab}$$

$$= \frac{c^2}{ab}$$



Ans ; B

12. given 1 minute $\rightarrow 360$ revolutions
 we have 1 revolutions $\rightarrow 2\pi$ radians
 360 revolutions $\rightarrow 720\pi$ radians
 $\therefore$ 1 minutes $\rightarrow 720\pi$
 60 seconds $\rightarrow 720\pi$
 1 second $\rightarrow \frac{720\pi}{60}$ radians
 1 second $\rightarrow 12\pi$

Ans : D

13. Given $\frac{2 \sin \theta}{1 + \cos \theta + \sin \theta} = x$

$$\Rightarrow \frac{2 \sin \theta}{(1 + \sin \theta) + \cos \theta} \times \frac{(1 + \sin \theta) - \cos \theta}{(1 + \sin \theta) - \cos \theta} = x$$

$$\Rightarrow \frac{2 \sin \theta (1 + \sin \theta - \cos \theta)}{(1 + \sin \theta)^2 - \cos^2 \theta} = x$$

$$\Rightarrow \frac{2 \sin \theta (1 + \sin \theta - \cos \theta)}{1 + \sin^2 \theta + 2 \sin \theta - \cos^2 \theta} = x$$

$$\Rightarrow \frac{1 + \sin \theta - \cos \theta}{1 + \sin \theta} = x$$

Ans : A

$$14. \quad \cos^4 \alpha + 2 \cos^2 \alpha (\sec^2 \alpha - 1)$$

$$= \cos^4 \alpha + 2 \cos^2 \alpha \cdot \tan^2 \alpha$$

$$= \cos^4 \alpha + 2 \cos^2 \alpha$$

$$= (1 - \sin^2 \alpha)^2 + 2 \sin^2 \alpha$$

$$= 1 + \sin^4 \alpha - 2 \sin^2 \alpha + 2 \sin^2 \alpha$$

$$= 1 + \sin^4 \alpha$$

Ans : A

$$15. \quad \text{Given } \tan 20^\circ = \lambda$$

$$\tan 160^\circ = \tan(180^\circ - 20^\circ) = -\tan 20^\circ = -\lambda$$

$$\tan 110^\circ = \tan(90^\circ + 20^\circ) = -\cot 20^\circ = -\frac{1}{\lambda}$$

$$\text{Now, } \frac{\tan 160^\circ - \tan 110^\circ}{1 + \tan 160^\circ \cdot \tan 110^\circ} = \frac{(-\lambda) - \left(-\frac{1}{\lambda}\right)}{1 + (-\lambda)\left(-\frac{1}{\lambda}\right)}$$

$$= \frac{1 - \lambda^2}{2\lambda}$$

Ans : C

$$16. \quad \text{given } \cos \theta > 0$$

$$\text{given } m = \tan \theta + \sin \theta$$

$$n = \tan \theta - \sin \theta$$

$$\text{now, } m+n = 2 \tan \theta, \quad m-n = 2 \sin \theta$$

$$\text{now } m^2 - n^2 = (m+n)(m-n)$$

$$= 4 \tan \theta \cdot \sin \theta \quad \dots(1)$$

$$\text{Option C } 4\sqrt{mn} = 4\sqrt{\tan^2 \theta - \sin^2 \theta}$$

$$= 4\sqrt{\sin^2 \theta \left(\frac{1}{\cos^2 \theta} - 1\right)}$$

$$\begin{aligned}
&= 4\sqrt{\frac{\sin^2 \theta (1 - \cos^2 \theta)}{\cos^2 \theta}} \\
&= 4\sqrt{\tan^2 \theta \cdot \sin^2 \theta} \\
&= 4\sqrt{mn} \quad \dots\dots(2) \\
&\text{from (1) and (2)} \\
&m^2 - n^2 = 4\sqrt{mn}
\end{aligned}$$

Ans : C

ADVANCED LEVEL QUESTION

17. Given $1 + \tan^2 \theta = \sec^2 \theta$

Option A : $\sec \theta = \pm \sqrt{1 + \tan^2 \theta}$, true

Option B : $1 + \tan^2 \theta = \sec^2 \theta$

$$\Rightarrow \tan^2 \theta = \sec^2 \theta - 1$$

$$\Rightarrow \tan \theta = \pm \sqrt{\sec^2 \theta - 1}, \text{ true}$$

Option C : $1 + \tan^2 \theta = \sec^2 \theta$

$$\Rightarrow \tan^2 \theta - \sec^2 \theta = -1, \text{ true}$$

Option D: $1 + \tan^2 \theta = \sec^2 \theta$

$$\sec^2 \theta - \tan^2 \theta = 1$$

$$\Rightarrow (\sec \theta + \tan \theta)(\sec \theta - \tan \theta) = 1$$

$$\Rightarrow \sec \theta + \tan \theta = \frac{1}{\sec \theta - \tan \theta}, \text{ true}$$

Ans : A,B,C,D

18. Given $\alpha = n\pi + \theta$

$$\Rightarrow \cos \theta = (-1)^n \cdot \cos \theta$$

Now, $\cos(3\pi + \theta) = (-1)^3 \cdot \cos \theta$

$$= -\cos \theta$$

Ans : B

$$\alpha = n\pi - \theta$$

$$\tan \alpha = -\tan \theta$$

19. $\tan(11\pi - \theta) = -\tan \theta$

Ans : C

20. $\cos(4\pi + \theta) \cdot \tan(4\pi - \theta)$

$$(-1)^4 \cdot \cos \theta - \tan \theta = -\cos \theta \cdot \tan \theta$$

$$= -\sin \theta$$

Ans : A

$$\begin{aligned} 21. \quad & \sec \theta (1 - \sin \theta) (\sec \theta + \tan \theta) \\ &= (\sec \theta - \sec \theta \cdot \sin \theta) (\sec \theta + \tan \theta) \\ &= (\sec \theta - \tan \theta) (\sec \theta + \tan \theta) \\ &= \sec^2 \theta - \tan^2 \theta \\ &= 1 \end{aligned}$$

Ans : 1

$$22. \quad \text{given } 4 \cot A = 3$$

$$\Rightarrow \cot A = \frac{3}{4}$$

$$\text{Now, } \frac{\sin A + \cos A}{\sin A - \cos A}$$

$$= \frac{1 + \cot A}{1 - \cot A}$$

$$= \frac{1 + \frac{3}{4}}{1 - \frac{3}{4}}$$

$$= 7$$

Ans : 7

$$23. \quad \text{a) We know } \sin^2 \theta + \cos^2 \theta = 1$$

$$= \sin^2 \theta = 1 - \cos^2 \theta$$

$$= 1 - \frac{1}{\sec^2 \theta} = \frac{\sec^2 \theta - 1}{\sec^2 \theta}$$

$$\therefore \sin \theta = \frac{\sqrt{\sec^2 \theta - 1}}{\sec \theta}$$

$$\text{b) } \cos \theta = \frac{1}{\sec \theta}$$

$$\text{c) } \sec^2 \theta - \tan^2 \theta = 1$$

$$\Rightarrow \tan^2 \theta = \sec^2 \theta - 1$$

$$\Rightarrow \tan \theta = \sqrt{\sec^2 \theta - 1}$$

$$\text{d) } \operatorname{cosec} \theta = \frac{1}{\sin \theta}$$

$$= \frac{\sec \theta}{\sqrt{\sec^2 \theta - 1}}$$

a-t, b-s, c-p, d-r

Additional Practice Question for students

1. Given $\sec A + \tan A = 3$ (1)

$\Rightarrow \sec A - \tan A = \frac{1}{3}$ (2)

(1) + (2) $\Rightarrow 2 \sec A = \frac{10}{3}$

$\Rightarrow \sec A = \frac{5}{3}$

Ans : B

2. Given $\tan^2 \theta = 1 - e^2$

$\Rightarrow \sec^2 \theta - 1 = 1 - e^2$

$\Rightarrow \sec^2 \theta = 2 - e^2$

Now $\sec \theta + \tan^3 \theta \cdot \operatorname{cosec} \theta$

$= \frac{1}{\cos \theta} + \frac{\sin^3 \theta}{\cos^3 \theta} \times \frac{1}{\sin \theta}$

$= \frac{1}{\cos \theta} + \frac{\sin^2 \theta}{\cos^3 \theta}$

$= \frac{\cos^2 \theta + \sin^2 \theta}{\cos^3 \theta} = \frac{1}{\cos^3 \theta}$

$= \sec^3 \theta$

$= (2 - e^2)^{\frac{3}{2}}$

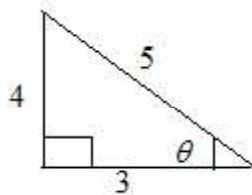
ANS : D

3. Given $\tan \theta = -\frac{4}{3}$

$\Rightarrow \theta \in Q_2 \text{ (or)} Q_4$

If $\theta \in Q_2$ then $\sin \theta = \frac{4}{5}$

If $\theta \in Q_4$ then $\sin \theta = -\frac{4}{5}$



Ans : B

4. $4(\sin^4 30^\circ + \cos^4 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ)$

$$= 4\left(\left(\frac{1}{2}\right)^4 + \left(\frac{1}{2}\right)^4\right) - 3\left(\left(\frac{1}{\sqrt{2}}\right)^2 - (1)^2\right)$$

$$= 4\left(\frac{1}{16} + \frac{1}{16}\right) - 3\left(\frac{1}{2} - 1\right)$$

$$= 4\left(\frac{1}{8}\right) + \frac{3}{2}$$

$$= \frac{1}{2} + \frac{3}{2}$$

$$= 2$$

Ans : 2

THE END

